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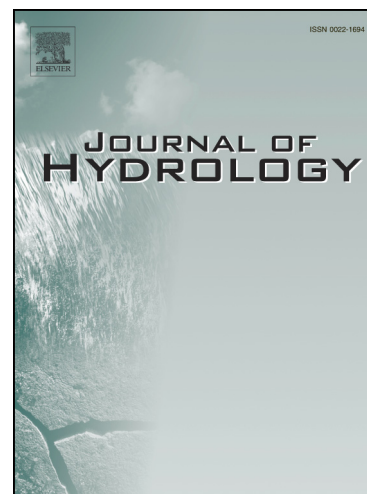
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1 Analysis of groundwater-level response to rainfall and estimation of annual 2 recharge in fractured hard rock aquifers, NW Ireland

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6 Abstract

7 Despite fractured hard rock aquifers underlying over 65% of Ireland, knowledge of key processes
8 controlling groundwater recharge in these bedrock systems is inadequately constrained. In this study,
9 we examined 19 groundwater-level hydrographs from two Irish hillslope sites underlain by hard rock
10 aquifers. Water-level time-series in clustered monitoring wells completed at the subsoil, soil/bedrock
11 interface, shallow and deep bedrocks were continuously monitored hourly over two hydrological
12 years. Correlation methods were applied to investigate groundwater-level response to rainfall, as well
13 as its seasonal variations. The results reveal that the direct groundwater recharge to the shallow and
14 deep bedrocks on hillslope is very limited. Water-level variations within these geological units are
15 likely dominated by slow flow rock matrix storage. The rapid responses to rainfall (≤ 2 hours) with
16 little seasonal variations were observed to the monitoring wells installed at the subsoil and
17 soil/bedrock interface, as well as those in the shallow or deep bedrocks at the base of the hillslope.
18 This suggests that the direct recharge takes place within these units. An automated time-series
19 procedure using the water-table fluctuation method was developed to estimate groundwater recharge
20 from the water-level and rainfall data. Results show the annual recharge rates of 42-197 mm/yr in the
21 subsoil and soil/bedrock interface, which represent 4-19% of the annual rainfall. Statistical analysis of
22 the relationship between the rainfall intensity and water-table rise reveal that the low rainfall intensity
23 group (≤ 1 mm/h) has greater impact on the groundwater recharge rate than other groups (> 1 mm/h).
24 This study shows that the combination of the time-series analysis and the water-table fluctuation
25 method could be an useful approach to investigate groundwater recharge in fractured hard rock
26 aquifers in Ireland.

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27 1. Introduction

28 Fractured plutonic and metamorphic rocks underlie over 65% of the island of Ireland. These hard
29 rocks with generally low groundwater yield are often referred to as poorly productively bedrock
30 aquifers (GSI, 2006; Robins and Misstear, 2000). Located in a temperate maritime climate where
31 surface water resources are abundant, these hard rock aquifers have attracted little research interest to
32 date in Ireland due to their limited role in public water supplies. As a result, knowledge of their role in
33 sustaining surface water quality and ecosystem services is poorly constrained, partly due to a lack of
34 detailed understanding of groundwater recharge processes, subsurface water movement within the
35 fractured bedrock system and stream-aquifer interactions. With the implementation of the European
36 Union Water Framework Directive (WFD), the Irish Environmental Protection Agency specifically
37 instrumented a number of hard rock aquifer sites as part of its groundwater monitoring network (Moe
38 et al., 2010). These instrumented sites were investigated as part of research activities funded under the
39 Irish National Geoscience Programme. This resulted in recent research publications characterising
40 hard rock groundwater systems using multi-scale hydrogeological and geophysical approaches
41 (Cassidy et al., 2014; Comte et al., 2012), as well as hydrogeochemical and mineralogical
42 investigations assessing groundwater contributions to river baseflows (Caulfield et al., 2014). Parallel
43 studies funded under the EPA Strive Research Programme focussed on pollutant pathways across
44 typical Irish catchment settings, including hard rock aquifer catchments (e.g. O'Brien et al., 2014).

45 In Ireland, groundwater recharge in hard rock aquifers has only received limited attention to date. A
46 small number of studies make reference to hard rock aquifers in terms of recharge and the variability
47 in hydrograph response between aquifer types (Misstear and Fitzsimons, 2007; Tedd et al., 2012).

48 Despite some site studies of recharge estimates for the fractured limestone aquifer and sand & gravel
49 aquifer (e.g., Misstear et al., 2009b; Misstear et al., 2008), the main focus of research activities in the
50 area of groundwater recharge over the last decade in Ireland was to develop a framework to assess
51 groundwater vulnerability. This framework was to account for key factors, including permeability and
52 thickness of superficial deposits, the presence of saturated soil and the hydrogeological properties of

53 the underlying aquifer, to produce the national groundwater recharge map (Fitzsimons and Misstear,
54 2006; Misstear et al., 2009a; Swartz et al., 2003; Williams et al., 2013).

55 Recently, an investigation of a headwater catchment underlain by the hard rock aquifer in Gortinlieve,
56 County Donegal, Ireland suggests that deep groundwater contributes to the maintenance of annual
57 river baseflow levels (Caulfield et al., 2014). Other field investigations of igneous rock (granite)
58 systems in Japan and USA have also reported that groundwater within the weathered bedrock zone
59 beneath the subsoil on hillslopes contribute 14-95% to streamflow generation (cf. Salve et al., 2012).
60 Studies in the UK and Australia reveal that there is significant groundwater flow through both shallow
61 and deep fractured bedrocks which could provide much of stream input even during periods of high
62 flow (Banks et al., 2009; Shand et al., 2007). Despite these studies providing different results with
63 regard to the role of shallow and deep groundwater for streamflow generation which probably reflects
64 specific differences in hydrogeological settings, all studies underline the importance of fractured hard
65 rock systems in terms of transferring water and associated pollutants (e.g., nitrate) to surface water
66 bodies (e.g., Paulwels et al., 2001; Pawar and Shaikh, 1995) . A better understanding of groundwater
67 flow pathways within the Irish hard rock systems could help to implement a programme of measures
68 to meet water quality targets required by the WFD.

69 To generate streamflow even at times of high flow, precipitation must transit the unsaturated zone of
70 the hard rock system and cause a rapid groundwater-level response for delivering water to bordering
71 streams. This is a function of groundwater recharge. To investigate how the hard rock system
72 contributes to streamflow generation, we must understand the recharge processes within different
73 geological units in the system. This requires monitoring installations within different geological zones
74 of the hard rock system to investigate groundwater-level response to rainfall as well as to estimate
75 recharge rates. There are a number of studies which have been reported using field instrumentation
76 techniques (tensiometers and/or piezometers) to investigate groundwater processes on hillslopes
77 underlain by the hard rock aquifers. Some focused on groundwater recharge (e.g., Kosugi et al., 2006;
78 Salve et al., 2012), others focused on flow at the soil/bedrock interface (e.g., McDonnell, 1990;
79 McGlynn et al., 2002) and aquifer-stream interactions (e.g., Banks et al., 2009; Tromp-van Meerveld

80 et al., 2007; Uchida et al., 2003). With the newly established groundwater monitoring network in
81 different hard rock aquifer settings across Ireland, hydrogeological data (e.g., well log data,
82 groundwater levels and water quality) from different geological units have been collected from dozens
83 of high-quality clustered monitoring wells. These hydrogeological data (e.g., groundwater-level time-
84 series) in combination with the rainfall data provide new information to advance the understanding of
85 key hydrological processes controlling groundwater flow and recharge in hard rock aquifers. These
86 advancements can be achieved by joint analysis of rainfall and groundwater-level time-series.

87 Correlation and spectral analyses of rainfall and groundwater-level time-series has been used to
88 identify recharge mechanisms in fractured aquifers (Chae et al., 2010; Jimenez-Martinez et al., 2013;
89 Lee and Lee, 2000). The advantage of this approach is its simplicity and the widespread availability of
90 groundwater-level data. The time-series analysis approach was introduced to investigate groundwater
91 flow regimes and aquifer storage capacity in karst aquifers. (e.g., Larocque et al., 1998, Mangin, 1984;
92 Padilla and Pulidobosch, 1995). The approach treats rainfall and spring discharge/piezometric level
93 time-series as input and output signals, respectively. While the karst aquifer is considered as a filter
94 which transforms, retains, or eliminates the input signal in the creation of an output signal. The
95 groundwater-level/spring discharge response to rainfall is one of the key results of the analysis.

96 Crosbie et al. (2005) later incorporated the time-series analysis approach into the water-table
97 fluctuation (WTF) method for groundwater recharge estimate. In the improved WTF approach, the
98 required time for groundwater-level response to rainfall (the time lag) was obtained from the
99 correlation analysis of the water-level and rainfall data. The rise of water-table during the time lag is
100 considered as a result of groundwater recharge. Groundwater recharge is estimated by the height of
101 water-table build-up during/after a rainfall event times the specific yield (Healy and Cook, 2002).

102 The objective of this study is to explore the usefulness of the time-series analysis and water-table
103 fluctuation methods to improve the understanding of groundwater recharge processes within the
104 different geological layers in hard rock aquifers in northwest Ireland, as well as to estimate annual
105 recharge rates. This is achieved by conducting correlation analyses of the groundwater-level time-
106 series, which are collected from clustered monitoring wells completed in the subsoil, at the

107 soil/bedrock interface, and in the shallow and deep bedrocks at two hillslope sites underlain by
108 fractured hard rock in northwest Ireland. The analysis of the groundwater-level response to rainfall
109 from the clustered monitoring wells at high, intermediate and low slope elevations at each site
110 improves the conceptual understanding of groundwater recharge in the different geological layers of
111 the hard rock system. An automated time-series procedure using the water-table fluctuation method is
112 developed to estimate annual groundwater recharge rates within the geological layers, where the
113 direct recharge processes have been identified by correlation analyses.

114 **2. Site descriptions and well instrumentation**

115 Two hillslope hard rock sites in the west and northwest of Ireland were selected for this study (Figure
116 1a-c). The west site located in Co. Mayo, Glencastle (GC), is underlain by a suit of the high grade
117 metamorphic gneisses, schists and quartzites. The northwest site located in Co. Donegal, Gortinlieve
118 (GO), is underlain by the intermediate grade metamorphic rocks of Precambrian piasammitic
119 micaschists, with occasional marbles of the Dalradian Southern Highland Group. The hydrogeological
120 characterisation of both sites has been carried out using various tools including surface geophysics,
121 downhole geophysics, single well tracer tests, hydraulic testing and fracture mapping (Comte et al.,
122 2012; Deakin et al. 2015, Ofterdinger et al. 2015; Nitsche 2014). According to the conceptualisation
123 of poorly productive aquifers in Ireland (Comte et al., 2012; Moe et al., 2010), four depth-dependant
124 lithological zones are commonly defined: 1) Subsoil (SS)-overburden deposits such as glacial till and
125 alluvium; 2) Transition Zone (TZ)- the overburden/bedrock interface containing highly permeable
126 decomposed and broken bedrock; 3) Shallow Bedrock (SB)-slightly permeable fractured and
127 weathered upper bedrock; and 4) Deep Bedrock (DB)-massive un-weathered bedrock. Figures 1d-e
128 show the schematic cross-section of the hydrogeological units represented by the four hydraulically
129 distinctive zones for both sites.

130 Both sites have been instrumented with three well clusters along a hillslope profile by the Irish
131 Environmental Protection Agency in 2006 as part of a wider groundwater monitoring programme.
132 Each well cluster consists of up to four screened or open-hole monitoring wells which were completed
133 within one of the hydraulically distinct zones of the bedrock aquifer (Figure 1d-e). The three well

134 clusters at each site constitute a linear transect at high (GC1 & GO1: 64 & 176 m amsl), intermediate
135 (GC2 & GO2: 30 & 89 m amsl) and low (GC3 and GO3: 18 & 34 m amsl) elevations. The depth of
136 the monitoring well varies from 2 to 79 m below ground surface. The summary of the well
137 specifications are detailed in Table A.1. The schematic cross-section of the monitoring wells
138 installation in the hydrogeological units is presented in Figures 1d-e.

139 **3. Data acquisition**

140 All the monitoring wells were instrumented with data loggers, which have been consecutively logging
141 groundwater levels on 15-minute intervals since late 2000s. During the period between October 2010
142 and September 2012, on a number of days no water-level records were available due to hydraulic tests
143 being completed in some wells. A linear interpolation was used to fill these data gaps in this study.

144 Rainfall measurements at the Gortinlieve site has been recorded by two automated tipping bucket rain
145 gauges (AEG 100) since October 2010, with one gauge installed at the high ground elevation close to
146 GO1 and another installed at the low ground elevation close to GO3. Rainfall was recorded in 15-
147 minute or one hour intervals. During the period between October 2010 and September 2012, there are
148 some short time periods without rainfall measurements due to blockage in the upper and/or lower rain
149 gauges. Missing rainfall measurements at each rainfall station were filled by measurements either
150 from the rain gauge at the top or at the base of hillslope in this study, respectively. For the periods
151 where no rainfall records were measured by the both rain gauges, these data gaps were filled by the
152 rainfall records from the Ballykelly weather station (Lon: $-7^{\circ} 1'$; Lat: $55^{\circ} 4'$; ~25 km northwest of
153 Gortinlieve, Figure 1a). As the Glencastle site is close to the Met Eireann synoptic station in
154 Belmullet (Figure 1a), rainfall measurements from the Belmullet synoptic station were used to
155 represent the rainfall in the Glencastle site. A previous study suggests a strong correlation between the
156 rainfall measurement on the site and the synoptic station (McGrath, 2008). Overall, the hourly rainfall
157 and groundwater-level data over two hydrological years (October 2010 to September 2012) were used
158 in this study.

159 **4. Time-series analysis**

160 **4.1 Auto- and cross-correlations**

161 Autocorrelation is the cross-correlation of a time-series with itself at different points in time. This
 162 function quantifies the linear dependency of successive values over a time period (Larocque et al.,
 163 1998) and investigates the “memory effect” (the required time for a system to “forget” its initial
 164 conditions) (Mangin, 1984). For an uncorrelated time-series (e.g., rainfall), the autocorrelation
 165 function exhibits a sharp decline from one to below a predefined value (usually 0.2) within a short
 166 time lag. In contrast, an autocorrelation function that exhibits a slow decline for a long time lag
 167 suggests that the time-series has strong interdependency and a long memory effect. The mathematical
 168 expression of the auto-correlation function can be written as:

169
$$C(k) = \frac{1}{n} \sum_{t=1}^{n-k} (x_t - \bar{x}) \cdot (x_{t+k} - \bar{x}), k \geq 0 \quad (1)$$

170
$$\gamma(k) = \frac{C(k)}{C(0)} \quad (2)$$

171 where $C(k)$ is the correlogram, n is the length of the time-series, k is the time lag ($k = 0$ to m ,
 172 $m \leq n/3$), x_t is the value of studied variables at time t , \bar{x} is the mean value of the series x_t , $\gamma(k)$ is
 173 the auto-correlation function.

174 The cross-correlation analysis considers transformation of the input to the output signals. The cross-
 175 correlation function represents inter-relationship between the input and output time-series. For a
 176 random input series, the cross-correlation function corresponds to the impulse response. For the cases
 177 where the cross-correlation function is not symmetrical and has a maximum or minimum for a
 178 positive lag, this indicates that the input signal has some impacts on the output signal. The lag time
 179 which corresponds to the maximum of the cross-correlation function is defined as the response time.

180 In this study, the response time obtained from the cross-correlation function between rainfall and
 181 groundwater-level time-series corresponds to the mean response time of the water-level in a well to
 182 rainfall events. This is similar to the concept which has been used to investigate discharge in the karst
 183 aquifers (e.g., Mangin, 1984). The mathematical expression of the cross-correlation function can be
 184 written as:

$$185 \quad C_{xy}(k) = \frac{1}{n} \sum_{t=1}^{n-k} (x_t - \bar{x}) \cdot (y_{t+k} - \bar{y}) \quad (3)$$

$$186 \quad \gamma_{xy}(k) = \frac{C_{xy}(k)}{\sigma_x \sigma_y} \quad (4)$$

187 where C_{xy} is the cross-correlogram, k is the time lag; n is the length of the time-series, x_t and y_t are
 188 input and output time-series, respectively, \bar{x} and \bar{y} are the mean values of the series x_t and y_t ,
 189 respectively, γ_{xy} is the cross-correlation function, and σ is the standard deviation of the time-series.
 190 To exhibit a significant correlation between input and output time-series at the 95% confidence
 191 interval, the cross-correlation function must have a correlation coefficient greater than the standard
 192 error $\sim 2/N^{0.5}$, where N is the number of values in the time-series data (Diggle, 1990; Lee et al., 2006).

193 4.2 Sliding window cross-correlation method

194 The cross-correlation analysis generally considers multi-year time-series data to reveal the general
 195 inter-relationship between input and output time-series over the data period. Delbart et al. (2014)
 196 proposed a sliding window cross-correlation method for the analysis of temporal variability of
 197 groundwater-level response to rainfall in a karst aquifer. This new cross-correlation method separates
 198 the whole input and output time-series data into sets of three-month data windows. Each data window
 199 has a one-and-a-half-month data overlap with its previous and/or following data windows and then the
 200 cross-correlation analysis is conducted for each data window to reveal the seasonal variability of the
 201 impulse response.

202 5. Water-table fluctuation method

203 The water-table fluctuation (WTF) method is based on the assumption that rises of the water-table in
 204 unconfined aquifers are attributed to recharge water arriving at the water-table. In the WTF method,
 205 groundwater recharge is estimated by the height of water-table build-up during/after a rainfall event
 206 times the specific yield (Healy and Cook, 2002). The mathematical expression can be written as:

$$207 \quad R = S_y \frac{\Delta h}{\Delta t} \quad (5)$$

208 where R is groundwater recharge; S_y is specific yield; and Δh is change in water-table height over the
 209 time interval Δt . Derivation of Equation (5) assumes that water arriving at the water-table goes

210 immediately into storage. This means that the impact of the lateral groundwater flow on water-level
 211 decline during a recharge event (drainage effect) is ignored, which could underestimate the actual
 212 recharge rate. Crosbie et al (2005) improved the WTF method to account for the drainage effect using
 213 the rainfall and groundwater-level time-series data. With accounting for the drainage effect, the
 214 groundwater recharge estimate in Equation (5) is revised for time-series data:

$$215 \quad R_t = \begin{cases} [(h_t - h_{t-1}) + D\Delta t]S_y & \text{if } \left\{ \begin{array}{l} [(h_t - h_{t-1}) + D\Delta t] > 0 \\ \text{and} \\ \sum_{t-t_r < t' < t} P_{t'} > 0 \end{array} \right. \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

216 where R_t is recharge at time t , h_t is water-level at time t , D is drainage rate (which accounts for how
 217 far the water level would have fallen had recharge not occurred), $P_{t'}$ is the sum of rainfall during the
 218 groundwater-level response time (t' , groundwater-level response time: the required time period to
 219 groundwater-level rise after a rainfall event which is determined by the cross-correlation analysis of
 220 the rainfall and groundwater-level time-series data).

221 The processes used in this study for the recharge estimate are summarised as: 1) determine the
 222 drainage rate as a function of the water-table height. Daily water-table decline rates at each well were
 223 determined by analysing the groundwater-level record of those days in the 2-year observation period,
 224 where no rainfall occurs during the day and its antecedent response time period. The drainage rate was
 225 determined by a linear fitting process of daily water-table decline to its corresponding water-table
 226 height; 2) add the drainage term into the hourly water-table change time-series with the antecedent
 227 rainfall ($P_{t'} > 0$); 3) conduct the cross-correlation analysis between the newly updated water-table
 228 change and rainfall time-series, and update the response time if it has been changed; this process is to
 229 account for the impact of the drainage effect on water-table change; 4) remove all negative terms in
 230 the water-table change time-series; 5) remove all positive terms with no antecedent rainfall ($P_{t'}=0$);
 231 this process is to eliminate/limit the impact of other factors (e.g., diurnal fluctuations and other factors)
 232 on recharge estimate; 6) aggregate the hourly positive water-table change time-series into a monthly
 233 time-series; 7) multiply the monthly water-table rise time-series by the specific yield to obtain the
 234 monthly recharge. In this study, a constant specific yield was to use for the recharge estimate, which

235 is different to the approach presented by Crosbie et al (2005) where a specific yield varying with
236 depth was applied.

237 Selection of appropriate values of specific yield for use in the WTF method is very challenging, in
238 particular for fractured hard rock aquifers. This is because aquifer tests for estimating specific yield
239 are usually unreliable for determining the specific yield in fractured rock systems due to the
240 limitations of the methods. These include the non-uniqueness of data interpretation as well as the
241 difficulty in verifying the validity of assumptions inherent in the techniques (Bardenhagen, 2000;
242 Freeze and Cherry, 1979). Specific yield obtained from other field methods for example the water-
243 budget method is considered to better represent the field conditions of fractured rock systems as this
244 does not require any assumptions concerning the flow processes (Healy, 2010). The detailed
245 discussions of selecting appropriate values for the recharge estimate and its limitations in this study
246 are presented in the later section (section 6.3).

247 **6. Results and discussions**

248 **6.1 Groundwater-level fluctuations**

249 Figures 2 and 3 show groundwater-level and rainfall time-series data at the Glencastle and Gortinlieve
250 sites over two hydrological years (October 2010 to September 2012). There are a total of 21
251 individual wells installed in clusters across both sites, monitoring groundwater level for specific depth
252 intervals and along differing hillslope elevations (Table A.1). However, only 20 water-level time-
253 series data are available as the well installed within the subsoil at the high elevation close to the top of
254 the hillslope at Glencastle (GC1-SS) was dry during this period. At Glencastle, water-level variations
255 over the two hydrological years show a distinctive pattern in each well cluster. The water-level in the
256 well cluster at the high elevation of the hillslope (GC1) shows a smooth and seasonal change between
257 recharge and recession periods with an annual variation of 4-5m. Water levels in the intermediate
258 elevation cluster (GC2) are remarkably stable throughout the year with an annual variation of less
259 than 0.35 m, while a 'flashy' hydrograph showing rapid responses to individual rainfall events was
260 observed in the low elevation cluster at the base of the hillslope (GC3) with an annual variation of less

261 than 0.6 m. The distinctive patterns of groundwater-level hydrographs in the three well-clusters at
262 Glencastle underlie different hydrogeological regimes influencing the groundwater flow and storage.

263 With GC1 installed in the mica schist and gneiss bedrocks without hydraulically active fractures
264 (CMD and OCM, 2010a), the smooth and seasonal change of groundwater hydrograph may indicate
265 that recharge in this bedrock unit is dominated by the slow flow pathways. These flow pathways are
266 likely controlled by the matrix flow which is similar to those reported in chalk aquifers (e.g., Ireson et
267 al., 2009). The upward head gradient at GC2 (Figure 2) suggests that the relatively high permeability
268 layer of the transition zone (5×10^{-2} m/d, Table A.1) may act as a conductive layer to drain the deep
269 groundwater towards the down gradient of the hillslope. This could result in the stable groundwater
270 levels throughout the year. Similar groundwater-level variations in shallow bedrock and transition
271 zone at this location indicate the hydraulic connection between the two units. No measurable changes
272 in groundwater-level within GC2-DB suggest that the well installed in the low permeable competent
273 gneiss bedrock (10^{-6} m/d, Table A.1) is isolated from the overlying units. The ‘flashy’ hydrographs
274 with the groundwater-level variations reflecting rainfall events at the base of the hillslope (GC3)
275 suggest a good hydraulic connection among the different hydrological units. The upward head
276 gradient and the lowest groundwater levels being maintained at a higher level than the nearby stream
277 level throughout the year indicate that both deep and shallow groundwater contribute to river
278 stormflow and baseflow.

279 Unlike the Glencastle site, groundwater hydrographs at Gortinlieve can be grouped into three
280 distinctive groups according to their variation patterns (Figure 3): 1) ‘flashy’ response to rainfall
281 across a number of recharge and recession events within a daily/weekly timeframe (GO1-TZ, GO2-
282 TZ and GO3); 2) smooth response to rainfall across recharge and recession events within a
283 weekly/monthly timeframe with seasonal variations (GO1-SB, GO2-SB and GO2-DB); 3) no
284 apparent response to the rainfall events but with the seasonal variations (GO1-DB). These different
285 variation patterns reflect the different hydrogeological settings where the wells have been installed. For
286 example, with GO1-TZ and GO2-TZ installed in the conductive transition zone (7×10^{-2} m/d, Table
287 A.1) overlain by a shallow 0.8 m subsoil, this geological setting supports rapid recharge and recession

288 responsive to the rainfall events. The relative high-conductive units at GO3 (subsoil: 10 m/d,
289 transition zone and bedrock units 3×10^{-3} - 4×10^0 m/d, Table A.1) suggest a good hydraulic connection
290 between the units at the base of the hillslope. As consequence of this, rapid and simultaneous
291 responses to rainfall events were found in all wells at the GO3 cluster. Similar to GC3, the upward
292 groundwater gradient and the higher groundwater level than the nearby stream level at GO3 indicate
293 that both deep and shallow groundwater contribute to stormflow and baseflow. At GO1, three
294 different types of groundwater hydrographs suggest different hydrological processes controlling
295 groundwater-level variations among the transition zone, shallow and deep bedrocks. In contrast, a
296 similar variation pattern in the shallow and deep bedrocks at GO2 may suggest similar hydrological
297 processes controlling groundwater level fluctuations in these two bedrock units. Despite GO1 and
298 GO2 being installed in similar bedrock units with similar permeabilities (Table A.1), the different
299 patterns of groundwater hydrographs in the shallow and deep bedrocks at these two well clusters
300 suggest that other factors apart from the rock permeability (e.g., topography and others) may also
301 influence on water-level responses to rainfall.

302 Overall, analyses of the groundwater hydrographs at the two study sites highlights that the processes
303 controlling groundwater-level response to rainfall are different in the different geological settings.
304 This implies that further analyses of the groundwater-level and rainfall time-series must be carried out
305 to identify the key recharge mechanisms in the different geological layers, before applying the
306 quantitative methods for recharge estimates. The analysis also suggests that deep and shallow
307 groundwater at the base of the hillslope contributes to stormflow and baseflow throughout the year. In
308 addition, the conceptual understanding of groundwater flow processes along the two hillslope sites
309 based on the measured water levels is presented by Figure A.1.

310 **6.2 Applications of the time-series analysis**

311 **6.2.1 Auto-correlation and data characteristics**

312 Auto-correlation analysis for the rainfall and groundwater-level time-series data can reveal the
313 structure of the data. This could help to identify if other hydrological processes have impacts on the
314 water-level variations. At Glencastle, the auto-correlation functions of the rainfall and groundwater-

315 level variations at the GC2 & 3 clusters decline quickly and reach a null value (Figure 4a). This is an
316 indicator of an uncorrelated characteristic of the hourly rainfall and groundwater-level variations over
317 the two hydrological years. Unlike GC2 & 3 clusters, groundwater-level variations at the GC1 cluster
318 show a very different behaviour, with the slow decline over a long time lag and the auto-correlation
319 function still above the critical value of 0.2 after 100 hours lag time. This represents a strong linear
320 inter-relationship and daily/weekly repetition behaviour of the variable. With the GC1 cluster being
321 installed in shallow and deep bedrock units without hydraulically active fractures (CMD and OCM,
322 2010a; Comte et al., 2012), the inter-relationship behaviour may suggest that the groundwater-level
323 variations are influenced by the rock matrix storage, where the slow flow pathways within the matrix
324 requires a long time to fill and drain the pores.

325 Unlike the Glencastle site, the auto-correlation functions at the Gortinlieve site are rather complex.
326 This includes: 1) an uncorrelated characteristic for rainfall as well as for the groundwater hydrographs
327 at GO1-TZ, GO2-TZ and GO3; 2) an inter-relationship behaviour for GO1-SB and GO2-SB; 3) a
328 periodic noise observed for GO1-DB and GO2-DB (Figure 4b). The uncorrelated characteristic at
329 GO1-TZ, GO2-TZ and GO3 indicates limited storage effect on the water-level variations at these
330 monitoring wells. This is consistent with the hydraulic test and well log data of the geological units
331 indicating that these wells were installed in relatively high permeability units (Table A.1). Similar to
332 those at GC1 (Figure 4a), the inter-relationship behaviour observed for the shallow bedrock at GO1-
333 SB & GO2-SB may suggest that groundwater-level variations are influenced by the rock matrix
334 storage within these units. A 24-hour periodic noise observed for the deep bedrock wells at GO1-DB
335 & GO2-DB may indicate an effect of diurnal tidal forcing (earth and/or atmospheric tides; Schulze et
336 al. 2000) on groundwater levels in these two deep bedrock wells.

337 **6.2.2 Cross-correlation and recharge implications**

338 Cross-correlation analysis was used to determine groundwater-level response time to rainfall, by using
339 the respective time-series data as the input and output signal. The mean response time represents the
340 lag time of the peak cross-correlation coefficient for the time-series data over the two hydrological
341 years. The seasonal response time was determined by the sliding windows cross-correlation method

342 which uses subsets of three-month data from the whole dataset. For the Gortinlieve site, the rainfall
343 time-series obtained in the rain gauge close to the top of the hillslope was used in the cross-correlation
344 analyses for GO1 & 2, while the measurements from the rain gauge at the base of the hillslope was
345 used for GO3.

346 At Glencastle, the cross-correlation functions show a good correlation (peak $\gamma_{P,\Delta h}$: ~ 0.5) between
347 rainfall and water-level variations for GC2-SS & -TZ and GC3 within a time delay of 1 hour, while a
348 fair correlation (peak $\gamma_{P,\Delta h}$: $\sim 0.2 \gg$ significant level of 0.015) was found for GC1 and GC2-SB with a
349 time lag of -1, -2 and 3 hours, respectively (Figure 5a & Table 1). The negative response time in
350 shallow and deep bedrocks at GC1 indicates that rainfall does not have a direct influence on the
351 groundwater-level fluctuation. This is consistent with the effect of the slow flow matrix storage
352 identified by the auto-correlation analysis (Figure 4a). The longer response time (3 hours) with a
353 lower peak value of $\gamma_{P,\Delta h}$ at GC2-SB than those (1 hour) for GC2-SS & TZ and GC3 may indicate
354 that, unlike the latter ones with the fast flow pathways for groundwater infiltration, the groundwater-
355 level fluctuation at GC2-SB has been influenced by vertical fast flow via hydraulic active fractures
356 combined with slow flow via the rock matrix within shallow bedrock unit. It is important to recognise
357 that, due to the scales of data plotting in Figure 2, water-level responses to rainfall look identical for
358 GC2-SS, TZ and SB. However, the hourly head response to rainfall over the two hydrological years at
359 GC2-SB is much smoother than those at GC2-SS and TZ (Figure S.1 in the supplement), which
360 attributes to a longer response time with a lower peak value of $\gamma_{P,\Delta h}$ at GC2-SB.

361 At Gortinlieve, the cross-correlation analysis reveals a rapid response to rainfall within 1-2 hours for
362 GO1-TZ, GO2-TZ and GO3, while a slow response up to 19 hours was found for GO1-SB and GO2-
363 SB. In addition, a negative response time of -60 hours with a low peak $\gamma_{P,\Delta h}$ value (0.05) for GO1-DB
364 and a response time of 26 hours for GO2-DB were observed (Figure 5b & Table 1). The rapid
365 response to rainfall at GO1-TZ, GO2-TZ and GO3 suggests that water-level fluctuations in these
366 wells are influenced by fast flow pathways. The slow response to rainfall at GO1-SB and GO2-SB
367 indicates that water-level fluctuations are influenced by slow flow matrix storage. For GO1-DB and

368 GO2-DB, the slow flow matrix storage and diurnal tidal forcing effects may be regarded as the main
369 reason for the negative and long response time.

370 Further analysis by the sliding window cross-correlation method shows that the seasonal variations in
371 rainfall have very limited impacts on the response times at the Glencastle site (Figure 6 & Table 1).

372 The results show high seasonal peak values of $\gamma_{P,\Delta h}$ (0.29-0.60) with the rather stable seasonal
373 response time observed at GC2-SS, GC2-TZ and GC3 regardless of varying rainfall intensity over the
374 two hydrological years (Figure 6c&d). This reiterates that groundwater infiltrations within these
375 geological units are dominated by fast flow pathways. For GC1, the relative stable negative seasonal
376 response time except for some variations between the end of 2010 and the beginning of 2011 (Figure
377 6b) again confirm that rainfall does not have a direct influence on the groundwater-level fluctuation.

378 The variations of the seasonal response times during the 2010 winter period are probably due to the
379 unusual heavy snow as a result of the unusual cold winter. The slow snow melting process in the
380 lower temperature of the hilltop could change the rainfall input into the aquifer. The seasonal
381 variability up to one order magnitude with the longer response times in the dry seasons and the shorter
382 ones in wet seasons at GC2-SB suggests a seasonal variability in the rock matrix storage. As water-
383 level at GC2-SB is higher than those at the shallow wells of GC2-SS and TZ, it is likely that the
384 seasonal variability was induced by the seasonal change of rock matrix storage up-gradient.

385 For the Gortinlieve site, the stable seasonal response time observed at GO2-TZ and GO3 with few
386 occasional outliers confirms that fast groundwater infiltration pathways are dominating within these
387 geological units again. However, there are some fluctuations observed in GO1-TZ, with a general
388 trend of a longer response times in the dry seasons and shorter ones in the wet seasons. This suggests
389 that the variations of the unsaturated thickness may have influences on seasonal groundwater
390 infiltration (Figure 7 & Table 1). As expected, with the storage effect on GO1-SB and GO2-SB as
391 well as tidal forcing effects observed in groundwater-level variations at GO1-DB and GO2-DB, a
392 larger seasonal variability of the response was found among these wells.

393 Overall the auto-and cross-correlation analysis reveal that groundwater infiltration at GC2-SS, GC2-
394 TZ, GC3, GO1-TZ, GO2-TZ and GO3 is dominated by fast flow pathways, with a limited seasonal
395 variability of the response time. In contrast, groundwater infiltration at GC1-SB, GC1-DB, GO1-SB
396 and GO2-SB is likely dominated by slow flow matrix storage. The groundwater variations in GO1-
397 DB and GO2-DB contain a periodic noise which may reflect the effect of tidal forcing
398 (earth/atmospheric). The seasonal change of matrix storage and tidal forcing effects may be regarded
399 as the main reasons for seasonal variability of the response time observed in these wells.

400 **6.3 Groundwater recharge estimate**

401 As the WTF method is based on the assumption that rises in water-table in unconfined aquifers are
402 due to direct recharge, we only use the groundwater hydrographs from 8 shallow wells (GC2-SS,
403 GC2-TZ, GC3-SS, GC3-TZ, GO1-TZ, GO2-TZ, GO3-SS and GO3-TZ) to estimate groundwater
404 recharge rates. In above correlation analyses, these wells showed water-level fluctuations dominated
405 by fast groundwater infiltration pathways. Despite a similar infiltration behaviour being identified for
406 GC3-SB, GC3-DB, GO3-SB and GO3-DB, these hydrographs have been not included in the recharge
407 estimates, as it is uncertain whether these bedrock units may be regarded as unconfined aquifer given
408 the observed upward head gradients.

409 Figure 8 shows the monthly accumulated water-table rise including the drainage term for the eight
410 shallow wells at Glencastle and Gortinlieve over two hydrological years applying the WTF method
411 (Equation 6). Overall the monthly water-table rises correlate well with the monthly rainfall for each
412 site, with a general trend of higher water-table rises occurring in wet winter months and lower ones in
413 dry spring/summer months. For the Glencastle site, similar water-table rises were observed for the
414 wells installed in the subsoil and transition zones of GC2 and GC3. This is an indication of these two
415 geological units being well connected as the hydrographs between SS and TZ were overlapped in
416 GC2 and GC3 (Figure 2) respectively. By using the same specific yield, the groundwater recharge
417 rates in the subsoil and transition zones at GC2 and GC3 are similar, despite the wells being installed
418 into different geological units but having water-level fluctuating within the subsoil layer (Table 2).
419 However, the monthly water-table rises at GC2 were only about a quarter of those further down the

420 hillslope at GC3. To determine the causes for this difference is difficult, given that both GC2 and GC3
421 are overlain by a sandy – clay layer with a similar thickness (3-4 m, Table A.1). One possible
422 explanation is the effect of the deep groundwater drainage towards the down gradient of the hillslope
423 induced by the upward gradient at GC2.

424 For the Gortinlieve site, the monthly water-table rises for individual well are rather complex. In
425 general, GO1-TZ is more responsive to rainfall than GO2-TZ, particularly in the wet season months.
426 This is consistent with the groundwater hydrographs, as groundwater fluctuations at GO1-TZ are
427 flashier than those at GO2-TZ (Figure 3). A similar pattern is also observed between GO3-SS and
428 GO3-TZ. In particular, the result shows that the increases of rainfall in some periods of the second
429 hydrological year (e.g., Oct-Dec 2011 and Jun-Jul 2012) has significant impact on the amount of
430 water-table rise (Figure 8b). An increase of annual rainfall of 26% in the second year led to the
431 increase of the annual water-table rise by 6.1 m for GO1-TZ, by 8 m for GO2-TZ, by 4.3 m for GO3-
432 SS and by 3.2 m for GO3-TZ when compared with those in the previous year (Table 2). The increase
433 in rainfall has more impact on groundwater recharge at locations with a thinner subsoil layer (0.8 m
434 for GO1-TZ and GO2-TZ, 3.3 m for GO3-SS and 4.8 m for GO3-TZ, Table A.1). This is consistent
435 with the previous study of the impact of subsoil thickness on recharge rates in Ireland (Missteart et al.,
436 2009a). Statistical analysis of the rainfall intensity shows that, despite an increase of ~250 mm rainfall
437 in the low intensity events (≤ 2 mm/h) for the second year, a similar distribution of the rainfall
438 intensity was found for the two hydrological years (Figure 9). There are some substantial increases of
439 the water-tables rises observed to GO1-TZ (3.5 m) and GO3-SS (~2 m) in low rainfall density events
440 (≤ 1 mm/h) in the second year. However, their contributions to the annual water-table rises in
441 percentage are similar to those in the previous year (~60%). In general, the low intensity rainfall
442 events (≤ 2 mm/h) contribute to ~65-70% of the annual rainfall, and contribute ~60-80% of the annual
443 water-table rise (Figures 9c & d). The increase of rainfall in the second year did not change the overall
444 distributions of the rainfall intensity events contributing to the annual recharge, except a 10% of the
445 annual recharge shifting towards the higher intensity rainfall events of ≥ 5 mm/h being observed in
446 GO3-TZ. The ratio of the water-table rise and rainfall show that the lower rainfall density group (≤ 1

447 mm/h) has higher impact on the groundwater recharge rate. The higher intensity groups (> 1 mm/h)
448 generally have a similar impact on groundwater recharge rate although some variations were found at
449 different wells.

450 Table 2 summarizes the annual recharge rates estimated by the WFT method, as well as the selected
451 specific yield values for recharge estimates. In this study, a specific yield of 0.01 and 0.005 was
452 chosen for the subsoil at both study sites and for the transition zone at Gortinlieve, respectively. These
453 values were obtained from studies of fractured rock site in east-central Pennsylvania (Gburek and
454 Folmar, 1999; Gburek and Urban, 1990; Heppner et al., 2007). The specific yield values were
455 obtained from the pan lysimeter measurements (e.g., water percolation rate) in the subsoil layers as
456 well as the combined analysis of the well hydrographs and the stream base-flow recession curve. The
457 similar values were also reported from another study of shale and limestone aquifers in Tennessee
458 using a similar method (Moore, 1992). We acknowledge that the selected specific yield of 0.01 for the
459 sandy-clay subsoil at Glencastle is slightly lower than those obtained from theoretical estimates (0.02-
460 0.07, Loheide et al., 2005) and field study in the South Eastern River Basin District in Ireland (glacial
461 till: 0.01-0.06, Tedd et al., 2012). In addition, the selection of appropriate values for specific yield for
462 the peaty clay subsoil layer in GC3 is very challenging, as few, if any, field observations of specific
463 yield of the peaty clay are available. Price and Schlotzhauer (1999) reported a specific yield of 0.048
464 for a mined peatland near Quebec, Canada. Loheide et al. (2005) also report the specific yield of 0.01-
465 0.07 for the different types of clay. As groundwater levels in the subsoil fluctuate within 0.5-2 m
466 below ground surface, a specific yield at the lower bound of reported values of 0.01 was selected to
467 estimate recharge rate in the subsoil to account for the likely capillary fringe effect. The selected
468 specific yield of 0.005 for the transition zone is an order of magnitude lower than the previous
469 reported value of storativity of 0.037 at Gortinlieve which was obtained from the pumping test
470 (Comte et al., 2012). Due to the drawbacks of pumping test to estimate specific yield in fractured rock
471 system (Bardenhagen, 2000; Freeze and Cherry, 1979), the estimated value was not used in this study.
472 Furthermore, the specific yield for the subsoil was used to estimate the recharge in transition zone of
473 GC2-TZ, GC3-TZ and GO3-TZ instead of using the specific yield for the transition zone. This is

474 because the groundwater-level fluctuations in these three wells are within its overlying subsoil layer
475 despite the wells being installed in the transition zone.

476 With the WFT method, annual recharge rates were estimated to be 48-175 mm/yr for the subsoil at
477 both sites (Table 2). These represent 5-19% of the annual rainfall. For the transition zone, the slightly
478 lower recharge rates of 42-159 mm/yr was obtained, which represent 4-17% of the annual rainfall.
479 The slightly lower recharge rates for the transition zone compared to the subsoil suggest that a small
480 percentage of the rainwater infiltration in the subsoil may travel down gradient via lateral flow within
481 the layer, which is consistent with general hillslope recharge mechanisms (e.g., Salve et al., 2012;
482 Uchida et al., 2003). The result also shows the spatial-temporal variations of the recharge rate for both
483 sites. In general, higher recharge rates are found at the base of the hillslope, while lower rates are
484 found at the hilltop and in the middle of the hillslope. Recharge rates at Gortinlieve are more sensitive
485 to the change of rainfall than those at Glencastle. An increase of the annual rainfall of 26% in the
486 second hydrological year led to the increase of the annual recharge rates of 40-90% at Gortinlieve
487 (Table 2). Overall, the spatial variation of recharge rates found at both sites is consistent with
488 findings from other studies, as recharge rates estimated from the WTF method can be influenced by
489 differences in elevation, geology, land-surface slope, and other factors (e.g., Lee et al., 2005).

490 We recognise that the recharge rates estimated in this study using the WTF method contains
491 uncertainty which is difficult to quantify. The major challenge of this study is that there was no
492 reported specific yield values obtained from the reliable field methods (e.g., the water budget method)
493 for hard rock aquifers in Ireland. In addition, there were very limited field-scale studies which have
494 been reported to estimate specific yield in the similar geological setting in other countries. Another
495 challenge of the study is to quantify the recharge rates within shallow subsoil and transition zones
496 where groundwater-level from ~0.5 m to 2m below ground surface. With such shallow depths of
497 water levels, the impact of the capillary pressure on specific yield estimate is dependent on the heights
498 of the capillary fringe in subsoil and transition zones. For the extreme cases where the depth to water
499 table is less than the height of the capillary pressure, no water is released when water levels change
500 (Childs, 1960; Healy, 2010). To quantify the uncertainty of the recharge estimates, field studies with

501 sophisticated field instrumentations (e.g., Gburek and Folmar, 1999; Gburek and Urban, 1990;
502 Heppner et al., 2007) are required to estimate specific yield for different geological units which was
503 beyond the scope of this study. In addition, it is important to recognise that the recharge rates
504 estimated for the shallow layers of subsoil and transition zones in this study do not necessarily
505 represent those in the deeper bedrock units. The low permeability of the deeper bedrock units can
506 prevent further vertical infiltration of rainwater. This is evident from the correlation analyses which
507 suggest that slow flow matrix storage controls water-level variations in shallow and deep bedrock
508 wells at the top and in the middle of the hillslope. The low permeability of the bedrock could induce
509 lateral water flow within the subsoil and transition zone, leaving only a small percentage of the
510 infiltrated rainwater further migration into the deeper bedrock via hydraulically active fractures and
511 slow flow pathways via the rock matrix.

512 **7. Conclusions**

513 In this study, we examined 19 groundwater level hydrographs from two Irish hillslope sites underlain
514 by hard rock aquifer. The correlation analyses of rainfall and groundwater-level variations show the
515 rapid groundwater-level response to rainfall (≤ 2 hours) with little seasonal variability at all the wells
516 completed in subsoil and transition zone as well as at wells installed in the shallow and deep bedrock
517 units at the base of the hillslope. This suggests that groundwater recharge in the subsoil and transition
518 zone as well as in the shallow and deep bedrock units at the base of the hillslope is dominated by fast
519 infiltration flow pathways. For wells completed in the shallow and deep bedrock units close to the
520 hilltop and at the middle of the hillslope, groundwater recharge in these shallow and deep bedrock
521 units at these locations is dominated by slow flow matrix storage.

522 A modified WTF method has been also applied to estimate groundwater recharge rate using the
523 groundwater-level and rainfall time-series in this study. In this approach, an automated time-series
524 computer code was developed for the recharge estimate by accounting for the drainage effect. In
525 addition, a procedure to examine the water-table rise by the antecedent rainfall was used to exclude
526 the water-table rises with no rainfall in the recharge calculation. This procedure was to eliminate/limit
527 the influences of diurnal fluctuations and other processes on recharge estimate. The results show

528 annual recharge rates of 48-175 mm/yr for the subsoil and 42-159 mm/yr for the transition zone.
529 These represent 5-19% and 4-17% of the annual rainfall rate, respectively. Statistical analysis of the
530 relationship between the rainfall intensity and water-table rise reveal that the low rainfall density
531 group (≤ 1 mm/h) has greater impact on the groundwater recharge rate than other rainfall groups (> 1
532 mm/h). This study showed the usefulness of the correlation analyses to characterise the groundwater
533 hydrograph and to understand the long-term and seasonal inter-relationship between groundwater
534 level variations and rainfall. This provides critical information to reveal the underlying processes
535 controlling water-level variations in the hard rock aquifers. Coupling the correlation analysis with the
536 automated WFT method could provide a useful tool to estimate recharge rates in the hard rock aquifer.

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706 recharge map for the Republic of Ireland. Quarterly Journal of Engineering Geology and
707 Hydrogeology, 46(4): 493-506. DOI:10.1144/qjegh2012-016

708 Table 1 Summary of cross-correlation and three-month sliding cross-correlation of rainfall and
 709 groundwater-level variations.

Site	Cluster	Well	Cross correlation ^a		Three-month sliding cross correlation			
			Peak $\gamma_{P,\Delta h}$	Lag-time (hrs)	Shortest lag-time (hrs)	Longest lag-time (hrs)	Max $\gamma_{P,\Delta h}$	Min $\gamma_{P,\Delta h}$
Glencastle	GC1	SB	0.21	-2	-1	73	0.29	0.09
		DB	0.21	-1	0	77	0.29	0.09
	GC2	SS	0.51	1	1	2	0.54	0.35
		TZ	0.47	1	1	3	0.50	0.29
		SB	0.22	3	11	2	0.32	0.17
	GC3	DB	NA	NA	NA	NA	NA	NA
		SS	0.50	1	0	1	0.58	0.33
		TZ	0.51	1	0	1	0.58	0.37
		SB	0.54	1	1	1	0.60	0.38
		DB	0.50	2	1	2	0.58	0.32
Gortinlieve	GO1	TZ	0.31	1	1	30	0.57	0.21
		SB	0.17	19	2	39	0.32	0.14
		DB	0.05	-60	0	-90	0.12	0.06
	GO2	TZ	0.48	1	1	18	0.69	0.33
		SB	0.21	17	3	22	0.34	0.20
		DB	0.12	26	10	73	0.24	0.09
	GO3	SS	0.46	1	1	3	0.68	0.43
		TZ	0.53	1	0	1	0.68	0.57
		SB	0.27	2	2	6	0.52	0.12
		DB	0.50	2	1	2	0.70	0.35

710 ^a correlation using data from the two hydrological years.

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712

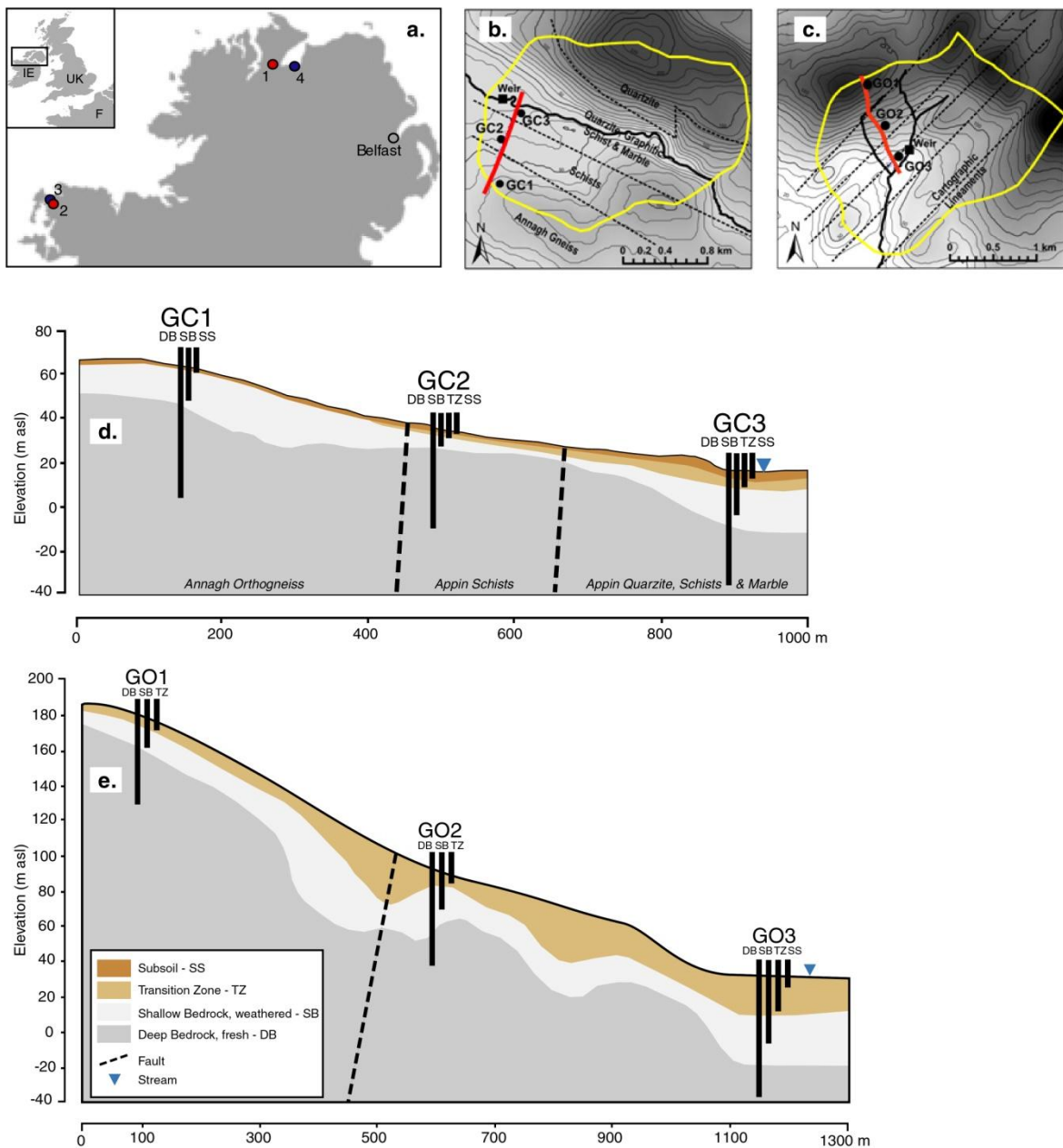
713 Table 2 Summary of groundwater recharge estimated by the WTF method

Year	Rainfall (mm/yr)	Water-table rise (m) / S_y				GW recharge (mm) / % of rainfall			
		GC2-SS	GC2-TZ	GC3-SS	GC3-TZ	GC2-SS	GC2-TZ	GC3-SS	GC3-TZ
10/11	831	4.8/0.01 ^a	5.0/0.01 ^b	14.7/0.01 ^a	13.7/0.01 ^b	48/6	50/6	147/18	137/16
11/12	924	4.8/0.01 ^a	5.1/0.01 ^b	17.5/0.01 ^a	16.0/0.01 ^b	48/5	50/6	175/19	159/17
		GO1-TZ	GO2-TZ	GO3-SS	GO3-TZ	GO1-TZ	GO2-TZ	GO3-SS	GO3-TZ
10/11	1134	13.6/0.005 ^a	8.8/0.005 ^a	7.4/0.01 ^c	4.2/0.01 ^c	68/6	44/4	74/7	42/4
11/12	1433	19.7/0.005 ^a	16.8/0.005 ^a	11.7/0.01 ^c	7.4/0.01 ^c	98/7	84/6	117/8	74/5

714 ^a Specific yield for sandy-clay and transition zone (Gburek and Folmar, 1999); ^b specific yield of sandy-clay used as the water-level fluctuation within the
715 subsoil layer; ^c Specific yield for peaty clay (Loheide et al., 2005; Price and Schlotzhauer, 1999).

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719 Figure 1: a) Location of study sites (1: Gortinlieve, 2: Glencastle) and meteorological stations (3:

720 Belmullet, 4: Ballykelly); Site layout maps of b) Glencastle site and c) Gortinlieve site indicating well

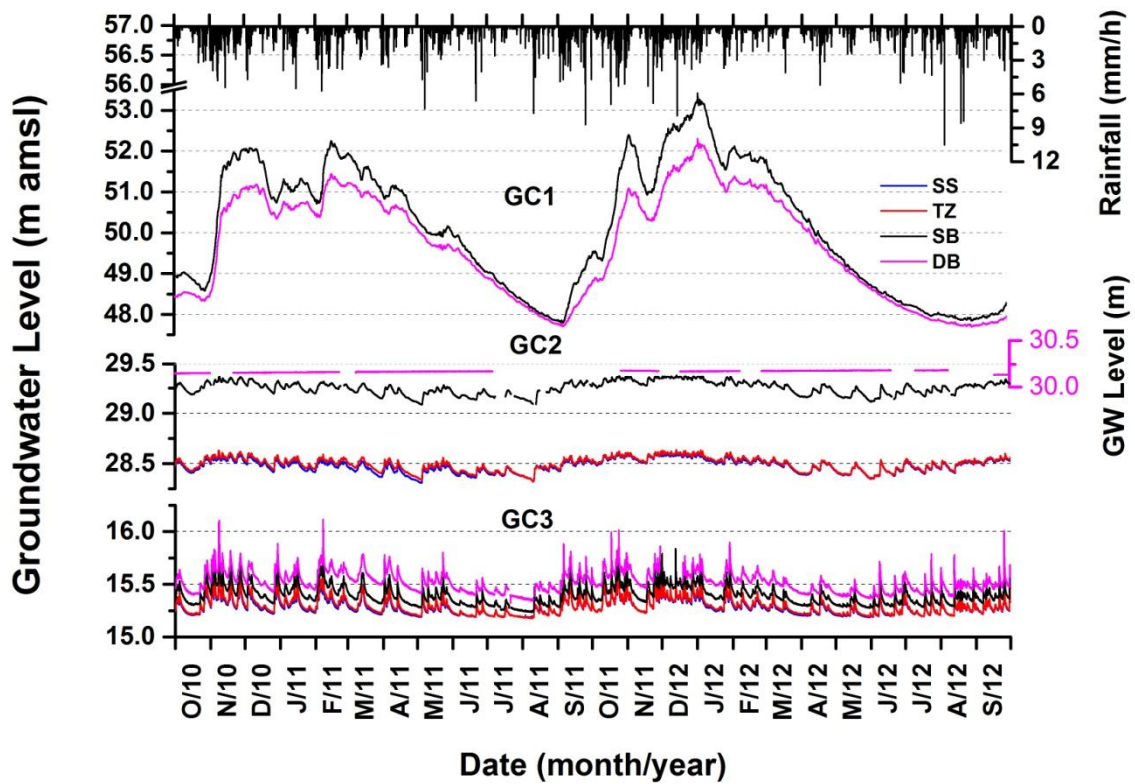
721 locations, structural lineaments, catchment boundaries (yellow) and profile sections (red); schematic

722 cross-sections of d) Glencastle site and e) Gortinlieve site, indicating nested well installation and key

723 geological zones as identified through electrical resistivity tomography and well log analysis (Comte

724 et al. 2012).

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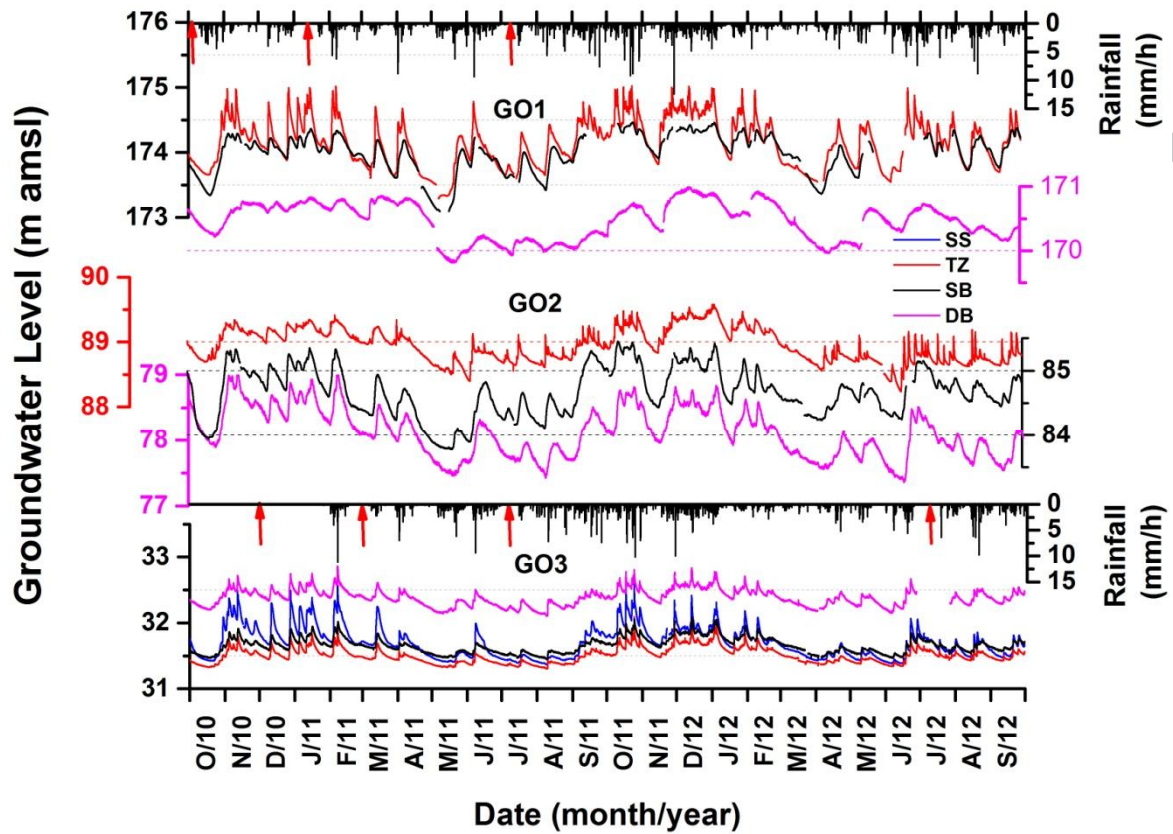
726

727 Figure 2. Rainfall and groundwater-level time-series in the Glencastle site. SS: Subsoil well; TZ:

728 Transition zone well; SB: Shallow bedrock well; DB: Deep bedrock well.

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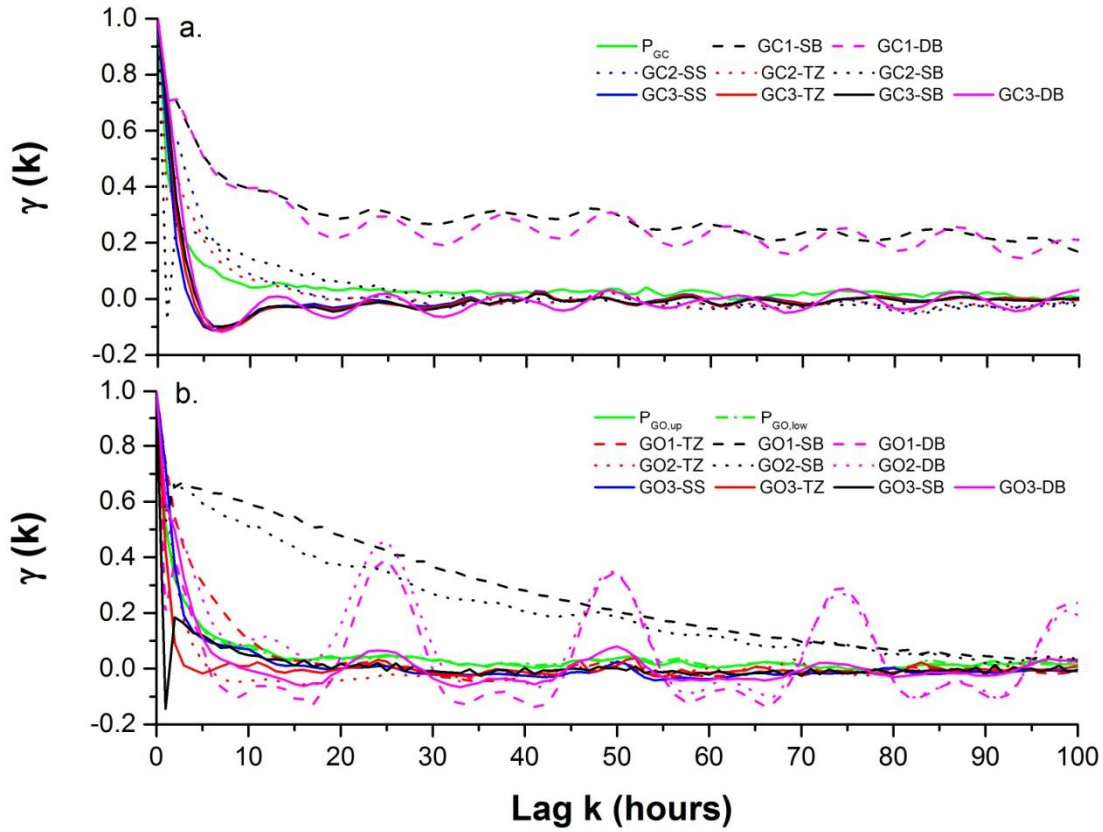
732 Figure 3. Rainfall and groundwater-level time-series in the Gortinlieve site. Note: red arrow pointing

733 at the periods with no rainfall records from the upper and/or lower rain gauges.

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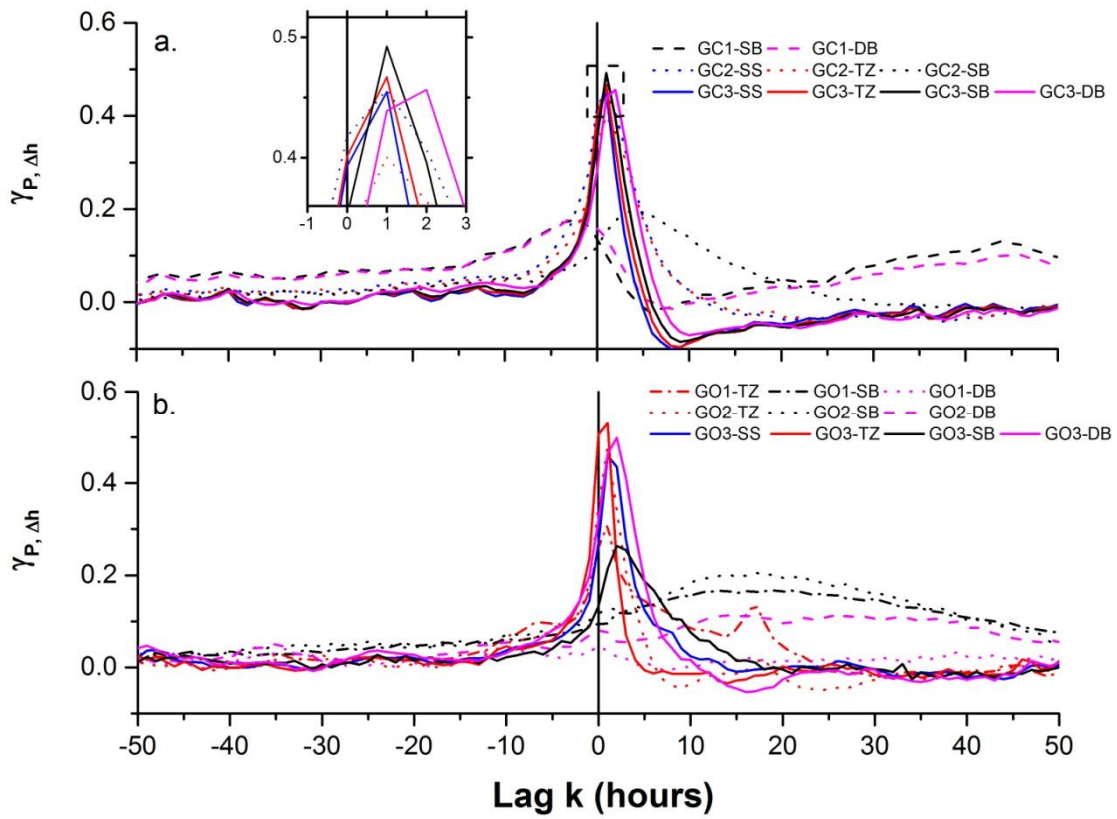


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738 Figure 4 Autocorrelation of rainfall and groundwater-level hydrographs in the Glencastle (a) and
 739 Gortinlieve (b) sites.

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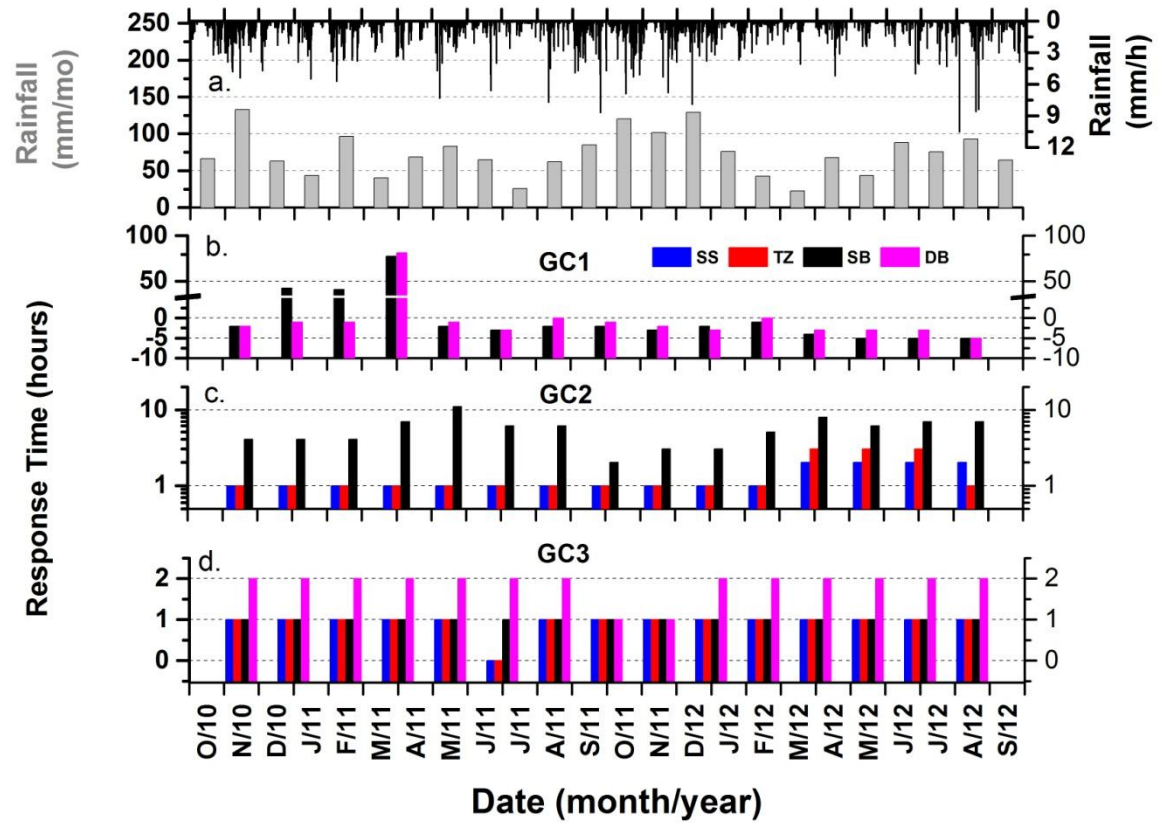


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743 Figure 5. Cross-correlation between rainfall and groundwater-level hydrographs at Glencastle (a) and

744 Gortinlieve (b) sites.

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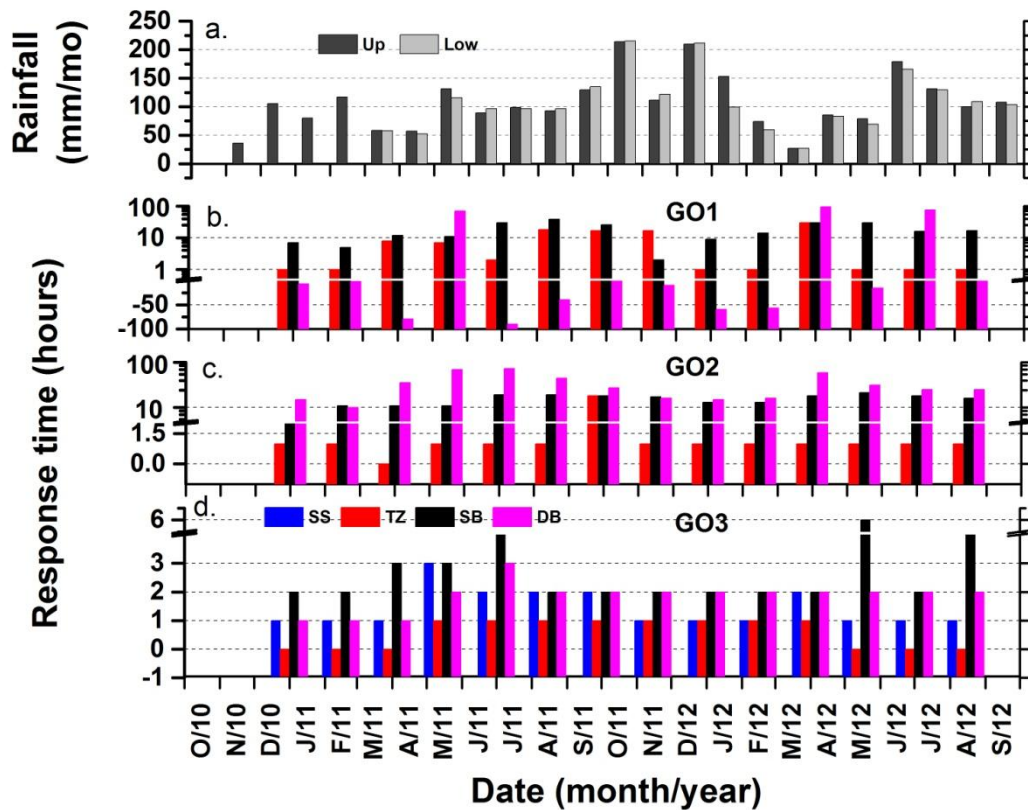


746

747 Figure 6. Rainfall (a) and the seasonal groundwater response time to rainfall in the Glencastle site (b-
 748 d). Note: Rainfall during the period from December 2010 to March 2011 was represented by snowfall
 749 due to the unusual cold winter.

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752

753 Figure 7. Rainfall (a) and the seasonal groundwater response time to rainfall in the Gortinlieve site (b-

754 d). Up: rainfall measurement in the hilltop; Low: rainfall measurement in the foothill. Note: 1) No

755 estimate of the seasonal response time in November 2010 as no rainfall measurements in the first 10

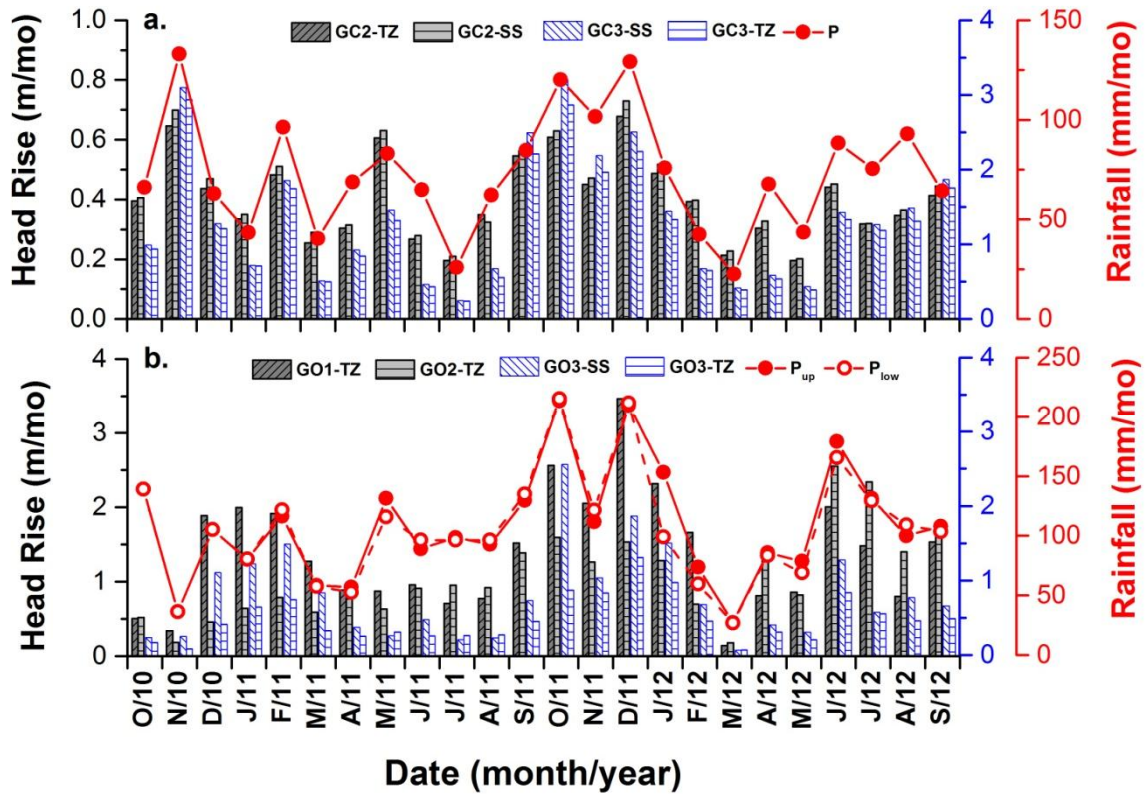
756 days in October 2010; 2) Rainfall during the period from December 2010 to March 2011 was

757 represented by snowfall due to the unusual cold winter.

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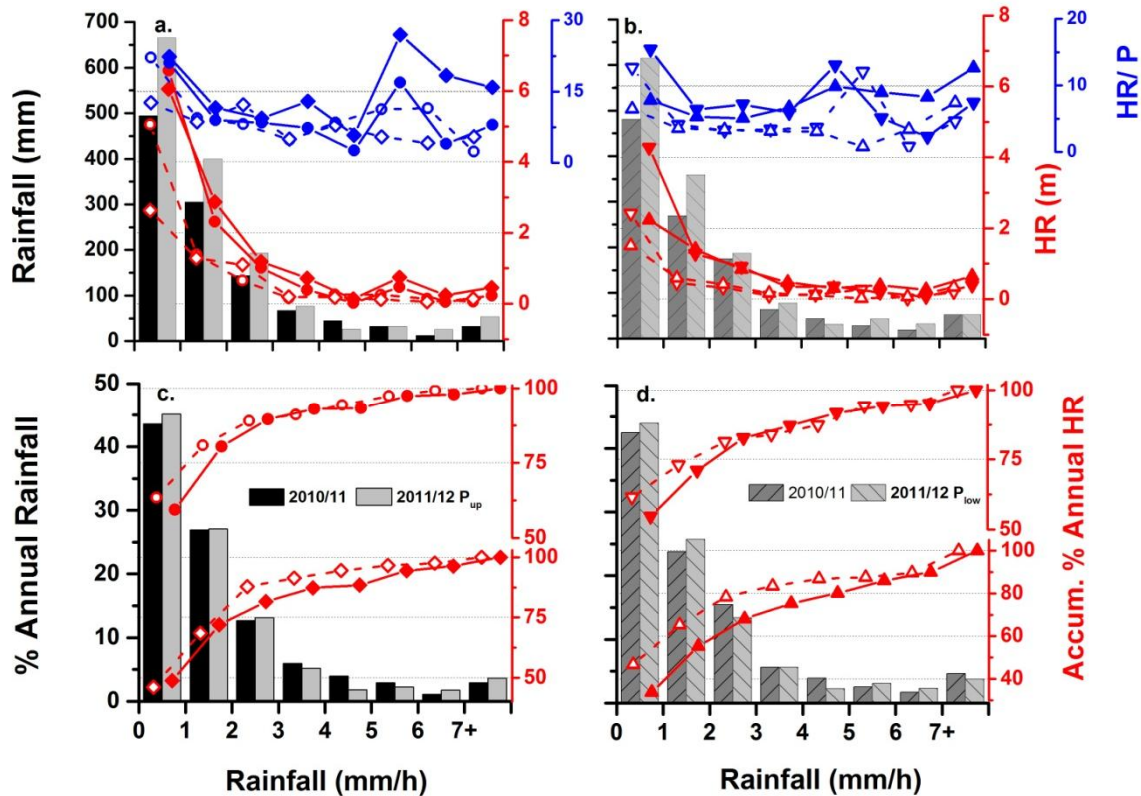
762 Figure 8. Monthly head rise estimated by the WFT method for the wells in the Glencastle (a) and

763 Gortinlieve sites (b) as well as monthly rainfall (P).

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768 Figure 9. Impact of rainfall (P) intensity on measured head rise (HR) in the Gortinlieve site. a & b: the
 769 amount of rainfall and head rise, as well as their ratio (HR/P). c & d: the annual proportion of the
 770 rainfall and the accumulative head rise. Legend: circle, GO1-TZ; diamond, GO2-TZ; down-pointing
 771 triangle, GO3-SS; up-pointing triangle, GO3-TZ; none fill colour symbol, 2010/11; fill colour symbol,
 772 2011/12.

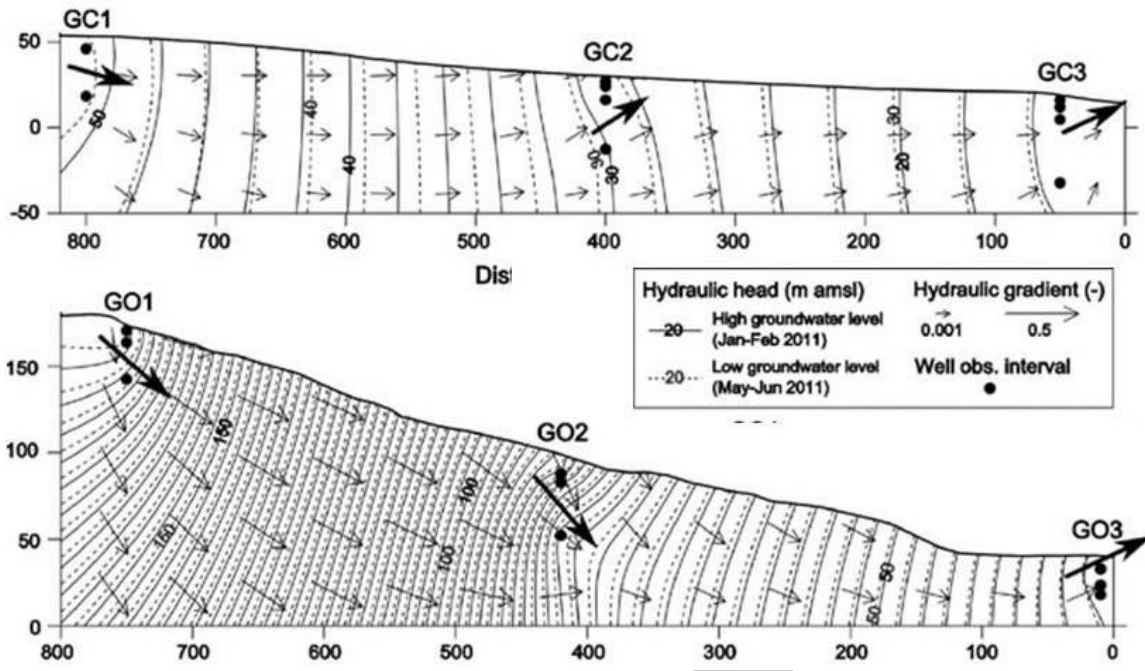
773

774 Appendix A

775 Table A.1. Well characteristics from driller's logs and aquifer permeability from pumping tests at the Glencastle and Gortinlieve sites.

	Cluster	Well	Depth (m) ^a	Well type	Well Interval (m bgl ^a)	Subsoil thickness (m)	Lithologies (m bgl ^a)	Permeability (K _h : m/d)
Glencastle ^b	GC1	SS	2.1m	6" screen	0.4-2.0	2.1	Poorly gravelly fine sand and trace till (0-2.1)	NA
		SB	22.9	6" open-hole	7.0-22.9	2.1	Weathered Schist (2.4-20.1),	5.6x10 ⁻³
		DB	61.0	6" open-hole	24.9-61.0	2.4	Gneiss: weathered (20.1-35.1), fresh (35.1-61).	1.6 x 10 ⁻³
	GC2	SS	4	6" screen	2.0-3.8	4.0	Poorly gravelly fine sand and trace till (0-4)	6.7x10 ⁻²
		TZ	7.1	6" screen	4.9-6.9	4.3	Slightly weathered gneiss (3.7-4.3),	5.1x10 ⁻²
		SB	20.4	6" open-hole	7.2-20.4	3.7	Gneiss: slightly weathered (4.3-8.5), fresh (8.5-20.4).	6.1x10 ⁻⁴
		DB	64.0	6" screen	21.3-64.0	4.3	Fresh gneiss (21.3-64)	1.1x10 ⁻⁶
	GC3	SS	3.1	6" screen	0.9-2.9	2.8	Poorly gravelly fine sand, cobbles and trace till (0-2.8)	4.5x10 ⁻²
		TZ	6.7	6" open-hole	4.4-6.7	3.4	highly & moderately weathered quartzite (4.4-6.7),	1.9x10 ⁻²
		SB	16.2	6" open-hole	10.4-16.2	2.7	Igneous rock: highly to moderately weathered (10.4-16.2)	1.3x10 ⁻¹
DB		78.9	6" open-hole	21.6-78.9	3.1	Quartzite: moderately to slightly weathered	3.7x10 ⁻⁴	
Gortinlieve ^c	GO1	TZ	2.5	6" screen	0.6-2.2	0.8	Peaty-clay (0-0.8); Psammite: heavily weathered with clay cover (0.8-1.5), weathered (1.5-2.4)	7.6x10 ^{-2d}
		SB	13.1	6" open-hole	4.7-13.1	0	Weathered Psammite (4.7-13.1), WS at 10	1.4x10 ⁻³
		DB	76.2	6" open-hole	46.8-76.2	0	Weathered/fresh Psammite (13.1-76.4), WS at 54 & 70.	6.6x10 ⁻³
	GO2	TZ	3.0	6" screen	0.6-2.8	0.8	Peaty and gravelly clay (0-0.8);	7.2x10 ⁻²
		SB	15.2	6" open-hole	7.9-15.2	1.2	Weathered Psammite (7.9-15.2), WS at 9 & 11.	2.0x10 ⁻³
		SD	67.1	6" open-hole	29.3-67.1	0.4	Fresh PsaPsammite, WS at 36	1.3x10 ⁻²
	GO3	SS	3.3	6" open-hole	1.6-3.2	3.3	Clay and peat (0-2.20), silt (2.2-3.4)	10 ^e
		TZ	7.1	6" open-hole	4.7-6.9	4.8	Heavily weathered Psammite with clay cover (4.8-6.7), WS at 5.2	4.8 ^d
		SA	23.4	6" open-hole	12.2-23.8	7.2	Weathered/fresh Psammite (8-23.4m), WS at 16 & 19	3.1x10 ⁻³
DA		53.3	6" open-hole	36.3-53.3	6.4	weathered/fresh Psammite (7.2-53.3m), WS at 24, 30 & 44	7.3x10 ⁻²	

776 ^a below ground level, ^b (CDM and OCM, 2010a); ^c (CDM and OCM, 2010b), ^d (Nitsche, 2014), ^e (Comte et al., 2012), WS: water strike

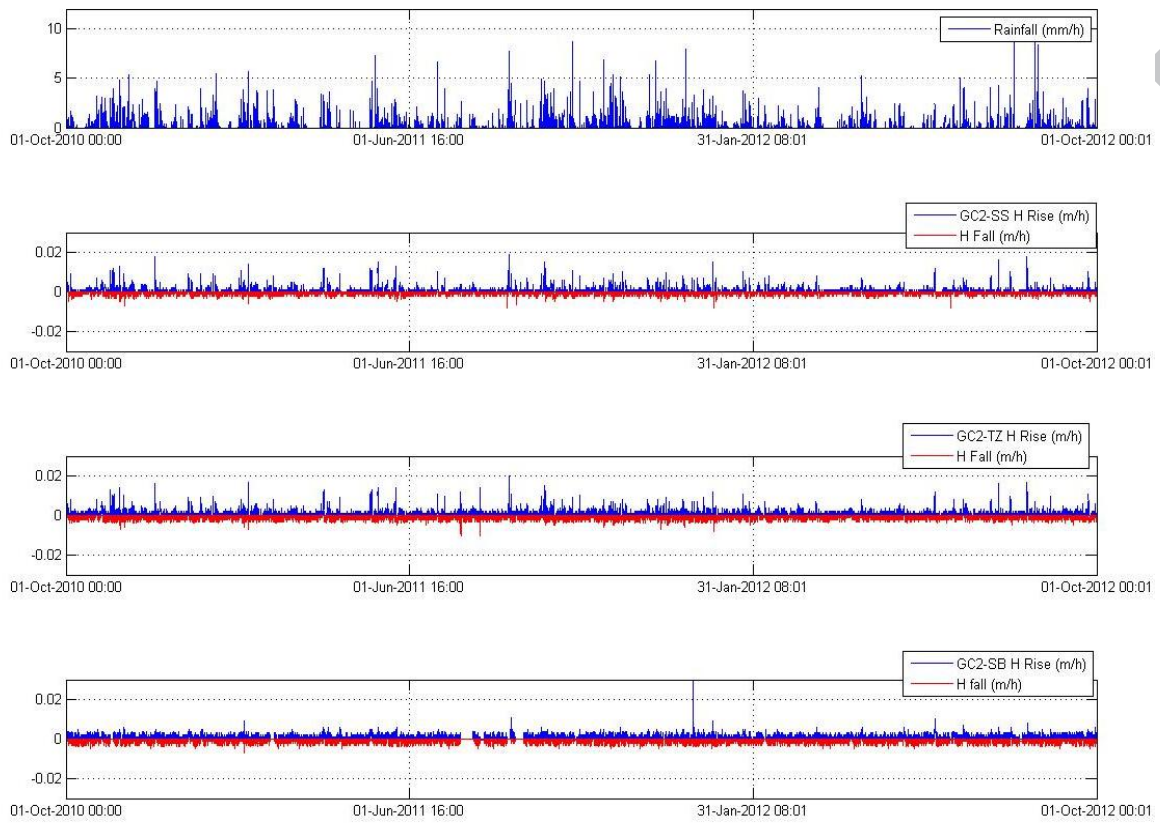


777

778 Figure A.1 Schematic representation of the groundwater flow processes along hillslopes towards the
 779 river (dist. river=0). The bold black arrows show the mean winter hydraulic gradients near the wells
 780 (after Comte et al., 2012).

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782 Supplement:



783

784 Figure S.1 Hourly rainfall and head changes at GC2-SS, TZ and SB over the two hydrological years.

Direct groundwater recharge to shallow or deep bedrocks on hillslope is very limited.

Direct recharge takes place within the subsoil and soil/bedrock interface.

Low intensity rainfall events (≤ 1 mm/hr) have higher impact on recharge rate.

Recharge rates of 42-197 mm/yr were estimated.

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