Conceptual Text Region Network: Cognition-Inspired Accurate Scene Text Detection

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Abstract

Segmentation-based methods are widely used for scene text detection due to their superiority in describing arbitrary-shaped text instances. However, two major problems still exist: (1) current label generation techniques are mostly empirical and lack theoretical support, discouraging elaborate label design; and (2) as a result, most methods rely heavily on text kernel segmentation which is unstable and requires deliberate tuning. To address these challenges, we propose a human cognition-inspired framework, termed, Conceptual Text Region Network (CTRNet). The framework utilizes Conceptual Text Regions (CTRs), which is a class of cognition-based tools inheriting good mathematical properties, allowing for sophisticated label design. Another component of CTRNet is an inference pipeline that, with the help of CTRs, completely omits the need for text kernel segmentation. Compared with previous segmentation-based methods, our approach is not only more interpretable but also more accurate. Experimental results show that CTRNet achieves state-of-the-art performance on benchmark CTW1500, Total-Text, MSRA-TD500, and ICDAR 2015 datasets, yielding performance gains of up to 2.0%. Notably, to the best of our knowledge, CTRNet is among the first detection models to achieve F-measures higher than 85.0% on all four of the benchmarks, demonstrating remarkable consistency and stability.

Keywords: Scene text detection, Arbitrary-shaped text detection, Neural networks, Semantic segmentation

1. Introduction

Scene text detection has received much attention from researchers because of its wide applications such as image translation, road sign recognition, and license plate reading. On account of the recent developments in object detection [1, 2] and semantic segmentation [3, 4, 5] based on Convolutional Neural Networks (CNNs) [6, 7], scene text detection has achieved substantial progress $[8, 9, 10, 11, 12, 13]$. Over the past few years, many deep learning-based methods have been proposed to conquer one of its most challenging tasks, arbitrary-shaped text detection. Among these methods, segmentation-based approaches [10, 11, 12, 13] have become the mainstream because such methods are more capable of describing text instances of irregular shapes. However, two major problems still exist: (1) current label generation techniques adopt rule-based algorithms [10] or simple operations such as polygon clipping [11, 13], which makes them mostly empirical and lacks theoretical support, discouraging elaborate label design; and (2) as a result, most methods [10, 11, 13] rely heavily on the unstable text kernel segmentation, which means directly segmenting the center lines of text instances, to separate adjacent text blocks. Such approach is deficient since it is prone to noise, as stated in [10], and requires deliberate tuning, as practiced in [11].

To settle these problems, we introduce a human cognitioninspired scene text detection framework called Conceptual Text Region Network (CTRNet) (see Fig. 1). It includes a class of

novel label generation tools termed Conceptual Text Regions (CTRs), a Feature Pyramid Network-based (FPN-based) [14] segmentation network, and a well-designed post-processing algorithm. Observing the solid advantages of introducing cognition-based computing [15, 16, 17], we design CTRs to represent the text instances inside our mind when we perceive arbitrary-shaped text instances. Specifically, as shown in Fig. 1 (c), a CTR is a well-defined rectangular area that mathematically inheres a smooth bijection from itself to the corresponding arbitrary-shaped text instance. The very bijectivity allows us to not only define with ease the width, height, and distortion of an arbitrary-shaped text instance but also transfer the geometric features defined within a CTR directly into its corresponding text instance (see Fig. 1). Afterwards, we utilize the segmentation network to learn the geometric features generated by CTRs in order to make predictions on unannotated images. Finally, a robust and interpretable post-processing algorithm makes full use of the geometric features and converts them into the detection result.

To demonstrate the effectiveness of our proposed CTR-Net, we conduct extensive experiments on four challenging benchmark datasets including CTW1500 [18], Total-Text [19], MSRA-TD500 [20], and ICDAR 2015 [21]. Among these datasets, CTW1500 and Total-Text are explicitly designed for arbitrary-shaped text detection. MSRA-TD500 and ICDAR 2015, on the other hand, focus on multi-oriented text. CTRNet consistently outperforms state-of-the-art methods on all four of the datasets in terms of F-measure, yielding performance gains of up to 2.0%. Notably, to the best of our knowledge, CTRNet

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Figure 1: Overview of the CTRNet framework. The red arrows represent the label generation process, during which the original text instances are mapped into their respective CTRs, and the geometric features are generated. The blue arrows, on the other hand, represent the network prediction pipeline, during which the segmentation network substitutes the functionalities of CTRs and predicts the geometric features, given only the original image as input. The black arrow represents the post-processing algorithm which converts the geometric features into the final detection result.

is among the first methods to achieve F-measures higher than 85.0% on all these datasets.

In summary, our contributions are threefold: (1) we propose CTRs as a class of well-designed label generation tools which inhere good properties such as bijectivity; (2) we propose a segmentation network and a post-processing algorithm that are capable of learning and processing geometric features, omitting the need for text kernel segmentation while establishing an accurate and interpretable inference pipeline; and (3) our CTRNet achieves state-of-the-art performances on a comprehensive set of benchmarks, showing great accuracy and consistency.

2. Related Work

Deep learning-based text detection methods have achieved outstanding results over the past few years. The majority of these methods utilize CNNs and can be roughly categorized into anchor-based methods and segmentation-based methods. In addition, it is of interest that text detection methods in general adopt specific and tailored label generation and postprocessing methodologies to utilize the geometric nature of text instances. Thus, we also introduce the label generation and post-processing techniques adopted by text detection methods.

2.1. Anchor-Based Methods

Anchor-based methods are often based on popular object detection frameworks such as Faster R-CNN [1] and SSD [2].

TextBoxes [22] modifies anchor boxes and convolutional kernels of SSD to handle the unique aspect ratios of text instances. TextBoxes++ $[23]$ further introduces quadrangle regression to allow for multi-oriented text detection. RRD [24] extracts rotation-invariant and rotation-sensitive features for text classification and regression respectively, eliminating the incompatibility between these two tasks when detecting multi-oriented text. RRPN [25], based on Faster R-CNN, developed Rotation Region Proposal Networks to detect multi-oriented text instances. SPCNet [26] and Mask Text Spotter [27] view text detection as an instance segmentation problem and utilize Mask

R-CNN [28] for arbitrary-shaped text detection. More recent anchor-based methods, such as Boundary [29], use Region Proposal Networks [1] and regression methods to obtain the boundary points of text instances and later rectify the detection results with differentiable operations such as Thin-Plate Splines (TPS) [30]. These structures include text recognition and enable the model to train in an end-to-end manner.

Anchor-based methods normally require few post-processing steps and perform reasonably well when handling multioriented text. However, most of them rely on complex multiple stages and hand-crafted anchor settings, which makes these approaches overcomplicated and less effective when handling long text instances.

2.2. Segmentation-Based Methods

Segmentation-based methods mainly view text detection as a segmentation problem and utilize Fully Convolutional Networks (FCNs) [3] or their variants.

Zhang et al. [31] first employ an FCN to extract text blocks and apply MSER to detect character candidates from the text blocks. Yao et al. [32] adopt an FCN to predict multiple properties of text instances, such as text regions and orientations. They then implement a clustering algorithm to obtain the detection result. PixelLink [33] performs link prediction to separate adjacent text regions. EAST [9] and DeepReg [34] detect the bounding boxes of words in a per-pixel fashion without using anchors or proposal networks. Newer segmentation-based approaches, such as TextSnake [10], PSENet [11], and PAN [13], detect arbitrary-shaped text instances through similar pipelines that involve text kernel segmentation and text reconstruction. Similar to anchor-based methods, there are also attempts to train segmentation-based models in an end-to-end manner. Text Perceptron [35], for example, adopts an FPN to predict fiducial points for TPS transformations.

Segmentation-based models are generally suitable for arbitrary-shaped text detection thanks to their flexibility. However, current approaches tend to endure less ideal label generation techniques and rely heavily on text kernel segmentation,

Figure 2: The inference pipeline of CTRNet. (a) The FPN-based segmentation network. The structure includes downsampling, upsampling, and the aggregation of features from different convolutional stages. For each input image, the network predicts 6 geometric features in a pixelwise manner. The produced feature map has 6 channels and is of the same width and height as the input image. (b) Illustration of the post-processing pipeline. Utilizing the predicted geometric features, a robust algorithm locates the text kernels and reconstructs the text instances. After post-processing, the detection result is obtained.

which is unstable and requires deliberate tuning. In contrast, our method includes CTRs, a class of well-designed tools for label generation, and omits the need for text kernel segmentation through elaborate label design.

2.3. Label Generation and Post-Processing Techniques

Text detection methods generally adopt tailored label generation and post-processing algorithms to make full use of the geometric nature of text instances. In particular, segmentationbased models tend to develop more sophisticated label generation techniques than anchor-based models and classical text detection methods.

Yin et al. [36] adopt multiple stages of post-processing steps including automatic threshold learning and machine learningbased text candidates filtering to refine the results generated by MSER. As a typical anchor-based method, RRPN [25] adopts a post-processing algorithm to compensate for the wrong detection results when handling long text instances. As for segmentation-based models, TextSnake [10] uses sophisticated label generation methods including a rule-based algorithm to extract text kernels. It later adopts a series of post-processing algorithms to reconstruct text instances and filter out false positives. PSENet uses polygon clipping for label generation. For post-processing, it utilizes an algorithm which expands the regions of the segmented text kernels to reconstruct the text instances. Moreover, according to its open-sourced official implementation, PSENet adopts a threshold-based filtering technique to filter out false positive predictions.

Current label generation and post-processing techniques generally take advantage of the geometric nature of text instances. However, the label generation methods are generally rule-based, and lacks theoretical support. Also, most postprocessing techniques do not utilize much of the geometric features of text instances. In contrast, the label generation process

of CTRNet is based on better mathematical principles, and its post-processing pipeline better utilizes the geometric features of text instances.

3. Methodology

In this section, we first introduce the inference pipeline of CTRNet. Next, we present the components of CTRNet, including the definition of a CTR, the network and label design, and the post-processing algorithm. Finally, the label generation process and the loss design are presented.

3.1. Inference Pipeline

The inference pipeline of the CTRNet framework is divided into two parts: a segmentation network and a post-processing algorithm (see Fig. 2).

We first employ an FPN-based segmentation network to predict 6 geometric features for each pixel, as shown in Fig. 2 (a). The post-processing algorithm later utilizes the geometric features and converts them into pairs of colinear offsets from text kernels and text edges, as illustrated in Fig. 2 (b). Using the offsets, the algorithm can easily locate the text kernels and reconstruct the text instances, obtaining the detection result.

For the details of the inference pipeline, Sec. 3.3.1 includes the specifics of the network structure, Sec. 3.3.2 explains the selection of the geometric features, and Sec. 3.4 contains a thorough introduction to the post-processing algorithm.

3.2. Conceptual Text Regions

In this section, we introduce Conceptual Text Regions, a class of human cognition-inspired tools aiming to describe the impression inside our mind when we conceive an arbitraryshaped text instance. We argue that such impression ought to be a text line of rectangular shape since it is the natural form

Figure 3: (a) Original text instance S . (b) Illustration of the triangulation and the prominent corner vertices. The prominent corners are highlighted in green. By our convention, $v_1 = v_{n+1} = v_{c_1}$. Please note that in our implementation, the triangulation has a maximum triangle area of 10^{-5} , which it is a lot denser.

of text and corresponds to the way we read. In addition, such impression should be smooth and invertible, since we are able to conceive every pixel within the text instance.

To achieve that, we develop a harmonic mapping-based rectifying method. The reason behind this choice is that harmonic mappings enable our proposed rectifying method to be smooth and bijective [37], while other rectifying methods, such as TPS, do not ensure bijectivity [38]. To prove the necessity of using harmonic mappings instead of TPS, a comprehensive ablation study is provided in Sec. 4.3.1.

We start with the construction of a harmonic mapping that maps an arbitrary text instance into an arbitrary rectangle. We first denote a rectangle of width w and height h by $R_{w,h}$. Afterwards, a harmonic mapping, denoted by $H_{w,h}$, which maps an arbitrary text instance S to $R_{w,h}$ is constructed as follows:

1. We first define a bijective boundary mapping

$$
b: \partial S \to \partial R_{w,h}, \tag{1}
$$

using the second boundary parameterization method described in Sec. 1.2.5 of [39]. The rationale behind this selection is that such method has good physical implications and ensures bijectivity [39].

2. $H_{w,h}$ is then obtained by solving the Laplace's equation

$$
\Delta H_{w,h} \equiv 0 \tag{2}
$$

subject to the continuous Dirichlet boundary condition

$$
H_{w,h}|_{\partial S} = b. \tag{3}
$$

To implement the above discussed procedure, we first obtain a refined triangulation T of an arbitrary-shaped text instance S using the constrained Delaunay triangulation method [40] with the maximum triangle area set to 10^{-5} (see Fig. 3 (b)). Second, we identify the four prominent corners of the text instance according to its reading sequence, which is illustrated as the green dots in Fig. 3 (b). Please note that this piece of information is provided in most text detection datasets, including the datasets we work with. Third, we obtain the boundary vertices, $\{v_1, ..., v_{n+1}\}\$, of triangulation T. For convenience, (1) $v_1 = v_{n+1}$;

(a) Text Instance S

(b) Rectangular Region $R_{w,h}$

Figure 4: (a) Original text instance S. The red lines and green lines represent the horizontal lines and vertical lines mapped from $R_{w,h}$, respectively. (b) A visualization of $R_{w,h}$. The red lines depict the horizontal lines, and the green lines depict the vertical lines. Please note that choosing a different set of w and h for $R_{w,h}$ does not affect this mapping of horizontal and vertical lines.

(2) v_1 is the top left corner; and (3) the vertices follow clockwise order. Fourth, we obtain the indices of the corner vertices. $\{c_1, c_2, c_3, c_4\}$, with $c_1 < c_2 < c_3 < c_4$. After these preparations, Algorithm 1 generates $H_{w,h}$ and $H_{w,h}^{-1}$. The Finite Element Method (FEM) [41] is used in this algorithm, and the implementation details of the FEM is provided in Sec. 4.2.

Following the Radó-Kneser-Choquet theorem [42, 43, 44], $H_{w,h}$ is bijective due to the convexity of $R_{w,h}$ [37]. With the help of $H_{w,h}$ and $H_{w,h}^{-1}$, we define the horizontal and vertical lines within S by constructing $H_{1,1}^{-1}: R_{1,1} \to S$ and afterwards mapping the horizontal and vertical lines within $R_{1,1}$ back into S.

Input: Triangulation: T Boundary vertices: $\{v_1, ..., v_{n+1}\}$ Corner indices: $\{c_1, c_2, c_3, c_4\}$ Target width and height: $\{w, h\}$ **Output:** $H_{w,h}$, $H_{w,h}^{-1}$

// Obtain the bijective boundary mapping b .

- 1: Define $b(v_{c_1})$, $b(v_{c_2})$, $b(v_{c_3})$, and $b(v_{c_4})$ as $(0, h)$, (w, h) , $(w, 0)$, and $(0, 0)$, respectively.
- 2: $c_5 := n + 1$ // It is for convenience.
- 3: for i in {1, 2, 3, 4} do

4: for
$$
j
$$
 in $\{c_i, c_i + 1, ..., c_{i+1} - 1\}$ do

5:
$$
b(v_j) := \frac{\sum_{k=c_i}^{y} ||v_{k+1} - v_k||}{\sum_{\substack{c_{i+1}-1 \ k=c_i}}^{z-1} ||v_{k+1} - v_k||} (b(v_{c_{i+1}}) - b(v_{c_i})) + b(v_{c_i})
$$

end for $6:$

 $7:$ end for

 $\frac{1}{2}$ Solve the Laplace's equation on T using the FEM.

- 8: $H_{w,h}(T) \coloneqq \text{FEM}(T, \Delta H_{w,h} \equiv 0, H_{w,h} |_{\partial T} = b)$
- // Obtain $H_{w,h}$ and $H_{w,h}^{-1}$ through interpolation.
- 9: $H_{w,h} =$ LinearInterpolation(*T*, $H_{w,h}(T)$)
10: $H_{w,h}^{-1} =$ LinearInterpolation($H_{w,h}(T)$, *T*)
-
- 11: **return** $H_{w,h}$, $H_{w,h}^{-1}$

Fig. 4 illustrates a visual explanation of this definition. Please note that the width and height of the rectangle $R_{w,h}$ do not affect this definition, thus, we select $R_{1,1}$ for convenience.

We may now define a CTR as R_{w_c, h_c} , where w_c and h_c are the average length of all horizontal and vertical lines within S , respectively. They can be calculated through the formulae:

$$
w_c = \iint\limits_{R_{1,1}} ||\partial_x H_{1,1}^{-1}(x, y)|| d\sigma , \qquad (4)
$$

$$
h_c = \iint\limits_{R_{1,1}} |\partial_y H_{1,1}^{-1}(x, y)| d\sigma . \tag{5}
$$

In our implementation, we calculate w_c and h_c through numerical integration.

We now conclude that, for any text instance S , there exists a unique CTR, that is R_{w_c,h_c} . It inheres the bijection $H_{w_c, h_c}: S \to R_{w_c, h_c}$. This means that for any given $(x, y) \in S$, there is a one-to-one corresponding $(x', y') \in R_{w_0, h_0}$, and vice versa. This property will be sufficiently utilized in Sec. 3.5 for label generation.

3.3. Network and Label Design

In this section, we explain in detail the architecture of our segmentation network and our label design.

3.3.1. Network Design

The purpose of the segmentation network is to predict the geometric features which can be later used. To achieve that, we adopt the well-tested FPN-based segmentation neural network. We now introduce the details of its architecture.

In a general sense, the segmentation network takes in an image of arbitrary shape and produces a feature map of the same width and height. The feature map has 6 channels, which corresponds to 3 classification results and 3 regression results.

Specifically, the detailed construction is demonstrated in Fig. 5. To ensure a fair comparison, we adopt the ResNet50 [6] as our backbone network, consistent to multiple recent works achieving state-of-the-art performances [11, 12, 13]. The ResNet50 structure is responsible for downsampling and is divided into 4 stages. Feature maps generated during downsampling are recorded and aggregated with their peer upsampling stages. To generate the prediction result, each one of the feature maps from the upsampling stages, illustrated in orange in Fig. 5, are upsampled and concatenated together. Finally, after a convolutional layer, a pixelwise prediction layer, and an upsampling layer, the prediction result is obtained.

To train the segmentation network, label design, label generation, and a loss function are needed. They are discussed in Sec. 3.3.2, Sec. 3.5, and Sec. 3.6, respectively. Besides, hyperparameters used to train this network in our experiments are unreservedly provided in Sec. 4.2.

Figure 5: Illustration of the segmentation network structure. Without loss of generality, we use an image of shape 512×512 as an example, although the input shape is not constrained. The convolutional kernel sizes are represented by " $1x1$ " or " $3x3$ ". The numbers after the convolutional stages are the output channel numbers, and the numbers after the upsampling stages are the scale factors. We use bilinear interpolation as the upsampling method to ensure smoothness.

3.3.2. Label Design

In this section, we design the geometric features that are learnable by the segmentation network and can be later converted into the offsets required by the post-processing algorithm.

For each point within a text instance, the post-processing algorithm takes in two colinear offsets and locates the corresponding text kernel and text edge. We represent each pair of those offsets with two colinear vectors $v_k = (r_k, \theta)$ and $v_e = (-r_e, \theta)$ (represented using the polar coordinate system), where v_k points to the text kernel, and v_e points to the text edge. Thus, for each pixel within a text instance, there is a corresponding pair of v_k and v_e .

For our segmentation network to predict a pair of v_k and v_e in a pixelwise manner, we design the labels with caution to ensure they are learnable by the network. Specifically, we first use one classification head to predict the text regions. Second, we adopt two regression heads to predict radiuses r_k and r_e . As for the angle θ , instead of predicting it directly like the text regions and the radiuses, it is conventional [10] to decompose it into

$$
\theta = \begin{cases} 2\arctan \frac{\sin \theta}{1 + \cos \theta}, & \text{if } \cos \theta \neq -1 \\ \pi, & \text{otherwise} \end{cases}
$$
(6)

Figure 7: Illustration of the clustering and reconstruction operations: (1) the larger circles represent p and the smaller circles represent either p_k or p_e ; (2) the red arrows depict v_k and the blue arrows depict v_e ; (3) the dashed arrows in (b) represent the extensions, which are of the same length as their corresponding v_k or v_e ; and (4) we use distinct colors to illustrate different clusters, and being gray means unclustered.

Figure 6: Illustration of the heat maps of α , sin θ , and cos θ . It can be observed in (b) that the heat map of α is generally smooth and continuous, whereas in (c) and (d), drastic jump discontinuity can be observed near the text kernels.

and predict $\sin \theta$ and $\cos \theta$ instead. However, in our case, the feature maps of $\sin \theta$ and $\cos \theta$ exhibit drastic jump discontinuity (see Fig. 6 (c-d)). Such discontinuity and rapid change make regression heads hard to train and yield inferior results [45, 46]. Numerical experiments proving this deficiency are provided in Sec. 4.3.2. Inspired by [46], we propose the reference anglebased encoding, which instead deconstructs θ into

$$
\theta = (-1)^{q_1} \alpha + (q_1 + q_2) \pi, \tag{7}
$$

where α is the reference angle of θ , and the combination of q_1 and q_2 depicts the quadrant that θ is located in. Specifically, q_1 is 0 if $\theta \in [0, \pi)$ and is otherwise 1. Likewise, q_2 is 0 if $\theta \in [\frac{\pi}{2}, \frac{3\pi}{2})$ and is otherwise 1. The motivation behind this transformation is to convert the regression target from the discontinuous θ into α , which is generally smooth and continuous within text instances (see Fig. $6(b)$), and handle the discontinuity through classification. We subsequently predict α , q_1 , and q_2 with one regression head and two classification heads, respectively. To summarize, we adopt three classification heads to predict text regions, q_1 , and q_2 , and we adopt three regression heads to predict r_k , r_e , and α .

3.4. Post-Processing

To acquire the detection result, a robust algorithm is introduced in this section to convert the geometric features predicted by the segmentation network into text predictions.

After prediction, the network produces 6 geometric features for each pixel, which are text regions, r_k , r_e , α , q_1 , and q_2 . To

begin with, we define the confidence value of a point as its confidence value for text region segmentation. As a preprocessing procedure, we first discard all points whose confidence value is lower than 0.65, and binarize q_1 and q_2 with a threshold of 0.5. For each remaining point, we then obtain its corresponding pairs of colinear vectors $v_k = (r_k, \theta)$ and $v_e = (-r_e, \theta)$, where θ is calculated through Eq. 7. Afterwards, the post-processing algorithm takes in all pairs of v_k and v_e . It is divided into three simple operations: clustering, reconstruction, and filtering.

3.4.1. Clustering

As shown in Fig. 7 (a), for the points within text instances, denoted by p , we first locate their corresponding kernel points, defined as $p_k = p + v_k$. Next, the connected-components algorithm is applied to all kernel points p_k , assigning a class to each kernel point. Finally, we let all p adopt the same class as their corresponding kernel points, forming distinct clusters.

3.4.2. Reconstruction

For each clustered point p , we first locate its corresponding kernel point, $p_k = p + v_k$, and edge point, $p_e = p + v_e$. Next, we further extend the line segment $\overline{p_k p_e}$ to restore the full height of the text instance, as shown in Fig. 7 (b). Finally, all points on the line segment are assigned the same class as the clustered point p , obtaining the reconstruction result.

3.4.3. Filtering

During clustering and reconstruction, rich information about the text instances are generated, which can be used to filter out false positives.

Specifically, for each text instance, we first define its confidence value as the average of the confidence values within it. Second, we define its distortion as σ_{α} , that is the standard deviation of all α values within the text instance. Third, we calculate its aspect ratio through formula $\frac{A}{4\mu_{r_k+r_e}^2}$, where A represents the area of the text instance, and $\mu_{r_k+r_e}$ is the average value of $r_k + r_e$ within the text instance. Please note that this formula gives a good estimation to the aspect ratio, because

$$
\frac{A}{4\mu_{r_k + r_e}^2} \approx \frac{w_c \cdot h_c}{4\mu_{r_k + r_e}^2} = \frac{w_c \cdot h_c}{\mu_{2r_k + 2r_e}^2} \approx \frac{w_c \cdot h_c}{h_c^2} = \frac{w_c}{h_c},\tag{8}
$$

where w_c and h_c are the width and height of the corresponding CTR. To better understand this approximation, please recall the definition of w_c and h_c explained in Sec. 3.2. Finally, we train a Support-Vector Machine (SVM) [47] taking the confidence values, distortion, and aspect ratios as features to filter out the false predictions.

The reasons behind the choice of an SVM instead of other techniques, for example a Deep Neural Network (DNN) [48], are twofold:

- 1. SVMs yield good performance with less data. In our case, the training samples are mostly identical, since most of the text instances are horizontal or alike. It results in a small amount of effective data. However, DNNs require a lot of data to avoid overfitting, while SVMs do not [49], thus SVMs are optimal in this case.
- 2. SVMs are easier to train. Unlike DNNs, SVMs generate training results quickly and deterministically [49]. Allowing us to adopt cross-validation to perform an efficient grid search for the optimal hyperparameters.

Compared with the conventional false positive filtering techniques that rely on hand-crafted thresholds for confidence and area values, as observed in TextSnake [10] and PSENet [11], our approach not only omits the need for human tuning but also leverages the more interpretable geometric information such as the distortion and aspect ratios.

An ablation study is carried out in Sec. 4.3.3 to evaluate our SVM-based filtering process and to validate the necessity of including the additional geometric information.

The implementation details of the SVM are provided in Sec. 4.2. Besides, a running time analysis for the SVM is carried out in Sec. 4.5.2.

3.5. Label Generation

In this section, we leverage CTRs to obtain the labels designed in Sec. 3.3.2, which are text regions, r_k , r_e , α , q_1 , and q_2 . For each point within a text instance, to calculate these geometric features, we need to first obtain its corresponding v_k and v_e . These offset vectors can then be converted into the geometric features with Eq. 7.

Specifically, for any text instance, it takes four steps: (1) defining the text kernel and text edge within its CTR, denoted by C_k and C_e ; (2) defining the offset vectors within its CTR, denoted by v'_k and v'_e ; (3) obtaining v_k and v_e by mapping v'_k and v'_e back into the text instance using H_{w_c,h_c}^{-1} ; and (4) calculating the geometric features using Eq. 7. Detailed explanations are provided below.

Figure 8: (a) Illustration of the text kernel and text edge defined within a CTR. The red and blue lines depict the text kernel and text edge, respectively. The black double-headed arrows indicate the lengths. (b) Illustration of the offset vectors defined within a CTR. The blue dots depict p' , the red arrows represent v'_{k} , and the blue dashed arrows represent v'_{e} .

3.5.1. Defining C_k and C_e

For any given text instance, we first obtain its CTR, denoted by C, and $C = R_{w_c, h_c}$, where w_c and h_c are calculated through Eq. 4 and Eq. 5.

It is trivial to define the text edge as $C_e = \partial C$. The text kernel, on the other hand, is defined as:

$$
C_k = \begin{cases} \{(x, y) | \frac{h_c}{2} \le x \le w_c - \frac{h_c}{2}, y = \frac{h_c}{2} \}, & h_c < w_c \\ \{(\frac{w_c}{2}, \frac{h_c}{2}) \}, & \text{otherwise} \end{cases}
$$
(9)

Fig. 8 (a) provides an illustration for the above definitions.

3.5.2. Defining v'_{k} and v'_{e}

For the CTR, C , we use p' to represent a point inside it. For each p' , it corresponds to a point in C_k and a point in C_e . They are denoted by p'_k and p'_e , respectively. For p'_k , it is defined as the nearest point to p' in C_k . For p'_e , on the other hand, it is defined as the intersection between C_e and a ray cast from p'_k through p' (see Fig. 8 (b)). We then define the offset vectors v'_k and v_e as:

$$
v'_k = p'_k - p',\tag{10}
$$

$$
v'_e = p'_e - p' \,. \tag{11}
$$

An illustration for the above definitions can be found in Fig. 8 (b).

3.5.3. Obtaining v_k and v_e

As explained in Sec. 3.2, a CTR naturally inheres a bijective harmonic mapping H_{w_c,h_c} that maps any point within its corresponding text instance into itself. With the help of H_{w_c, h_c} , mapping v'_{k} and v'_{e} back into the original text instance is as simple as:

$$
v_k = H_{w_c, h_c}^{-1}(p'_k) - H_{w_c, h_c}^{-1}(p'),\tag{12}
$$

$$
v_e = H_{w_c, h_c}^{-1}(p'_e) - H_{w_c, h_c}^{-1}(p'). \tag{13}
$$

Please note that after this mapping, v_k and v_e do not theoretically ensure collinearity. However, the variance is generally unnoticeable. Due to this reason, for $v_k = (r_k, \theta_k)$ and $v_e = (r_e, \theta_e)$, we use $v_e = (-r_e, \theta_k)$ to approximate the latter. The approximation is reasonable, since it hardly sacrifices any precision, and is necessary since our segmentation network is designed to handle colinear vectors. After this approximation, we use θ to represent θ_k for simplicity.

3.5.4. Obtaining the Labels

For the given text instance, we have obtained all of its v_k and v_e . We now utilize Eq. 7 to convert them into the trainable geometric features required by the segmentation network.

Specifically, for each point within the text instance, denoted by p, its corresponding offsets are $v_k = (r_k, \theta)$ and $v_e = (-r_e, \theta)$. We first set the value for text regions as 1, at point p . Second, the features r_k and r_e are naturally obtained from the above expressions. Third, according to Eq. 7, we can deconstruct θ into $(-1)^{q_1}\alpha + (q_1 + q_2)\pi$, thus obtaining the values for α , q_1 , and q_2 , at point p .

To be complete, for the points that are not included in any text instance, the values for text regions are set to 0, and the values for the other geometric features are set to -1, since they are undetermined.

3.6. Loss Function

In this section, we introduce the loss function adopted to train the segmentation network.

The loss function can be formulated as:

$$
L = \lambda L_{\text{text}} + (1 - \lambda)(L_{\alpha} + L_{q_1} + L_{q_2} + L_{r_k} + L_{r_e}),\tag{14}
$$

where λ balances the importance of L_{text} . The binary crossentropy loss is adopted for L_{text} , L_{q_1} , and L_{q_2} , and the Smooth-L1 loss is selected for L_{α} , L_{r_k} , and L_{r_e} , to ensure a more stable training process [1]. To overcome the data imbalance problem when segmenting text regions, we adopt OHEM 3:1 [50] for L_{text} . Please note that all losses except for L_{text} are set to 0 outside text instances, since the geometric features are undefined there.

4. Experiments

In this section, we first conduct a comprehensive ablation study for CTRNet. Then we evaluate the proposed method on four challenging public benchmarks: CTW1500, Total-Text, MSRA-TD500, and ICDAR 2015 to compare with other stateof-the-art methods. Finally, the overall results and running time analysis are presented.

4.1. Datasets

4.1.1. CTW1500

CTW1500 is a challenging dataset mainly focuses on long curved text instances. It consists of 1,000 training images and 500 test images, with each image containing at least 1 curved text instance.

4.1.2. Total-Text

Total-Text consists of word-level curved text instances. Horizontal, multi-oriented text instances are also included. It consists of 1,255 training images and 300 test images.

4.1.3. MSRA-TD500

MSRA-TD500 is a multi-language dataset that focuses on long multi-oriented text instances. It includes 300 training images and 200 test images.

4.1.4. ICDAR 2015

ICDAR 2015 focuses on incidental scenes that mainly consists of word-level multi-oriented text instances. It has 1,000 training images and 500 test images.

4.1.5. ICDAR 2017

ICDAR 2017 MLT [51] is a multi-language dataset including 9 languages representing 6 different scripts. There are 7,200 training images, 1,800 validation images and 9,000 test images in this dataset. We use this dataset only for pre-training.

4.2. Implementation Details

We use ResNet50 pre-trained on ImageNet [52] as our backbone. All networks are trained with a batch size of 32 on 4 GPUs and tested with a batch size of 1 on a RTX2080Ti GPU. The optimization is done by using Adam optimizer [53] with the default beta values of $(0.9, 0.999)$.

The data augmentation techniques adopted are (1) random rotation within range $[-10^{\circ}, 10^{\circ}]$; (2) random resizing with ratio 0.75, 1.0, or 1.25; (3) random cropping of size 512×512 ; (4) random flipping; and (5) random color jittering.

During training, the λ for loss balancing is set to 0.67 and the negative-positive ratio of OHEM is set to 3. Following [11], we pre-train our model on ICDAR 2017 MLT for 50K iterations with a learning rate of 1×10^{-3} . We fine-tune the pre-trained model on each benchmark dataset for 10K iterations with a learning rate of 1×10^{-5} and compare the performance against other state-of-the-art methods. For CTW1500 dataset specifically, we also train it from scratch for 10K iterations with a learning rate of 1×10^{-4} to convey a fair comparison against other methods that do not utilize external data.

During both training and inference phase, all images are proportionally resized to ensure a suitable shorter side length (736) for ICDAR 2015 and 640 for others).

For the construction of CTRs, we use scikit-fem [54] to implement the FEM and solve the Laplace's equation. All of the partial differential equations are solved with the results recorded before training to ensure a faster training process.

The SVM adopts the Radial Basis Function (RBF) [55] kernel, and its hyperparameters C and gamma are tuned through grid search within sets $\{0.1, 1, 10, 100\}$ and $\{1, 0.1, 0.001, 0.0001, 0.00001\}$, respectively. We use 5-fold cross-validation to evaluate each pair of the hyperparameters. The training data for the SVM is generated by running the segmentation model on the training set after each training epoch, so there is no test data leakage during the process.

4.3. Ablation Study

We conduct a comprehensive ablation study on CTW1500 and ICDAR 2015 datasets to demonstrate the effectiveness of our framework design.

4.3.1. Harmonic Mappings

We now explain the necessity of using harmonic mappings instead of TPS to construct CTRs.

Figure 9: Comparison between the TPS method and our proposed harmonic mapping-based method. "HM" indicates harmonic mappings. It can be observed in (a) that the results of harmonic mappings fit the target rectangle perfectly, also they are smoother and more uniform. In contrast, the rectifying results of TPS in (b) are irregular, and they do not fill in the whole rectangle region.

Figure 10: Comparison between the TPS method and our proposed harmonic mapping-based method. "HM" indicates harmonic mappings. It can be observed in (a) that the feature maps produced by harmonic mappings are smooth, and the text kernel location is accurate. However, in (b), the feature maps endure defects such as abrupt jump discontinuity, and the kernel location results are disordered.

From a theoretical perspective, TPS does not promise bijectivity [38], and there is no simple condition that can ensure a bijective TPS transformation. Thus, it is impossible for TPS to map the geometric features back into the arbitrary-shaped text instances without relying on complicated rules. In comparison, a harmonic mapping-based transformation is bijective as long as the target polygon is convex [37], which is not only elegant but also consistent to our needs. Fig. 9 shows the quality difference between our bijective harmonic mapping-based method and the TPS method.

From a practical perspective, although TPS performs well in many end-to-end text recognition tasks [29, 35], it is not suitable for our CTRNet framework which requires a refined mapping. To show that, we first adopt the nearest-neighbor interpolation method to process the irregular results generated by the TPS transformation. Second, distinct negative effects on the inference pipeline caused by the TPS method can be observed in Fig. 10. Third, the numerical experiments prove our standpoints. As shown in Tab. 1, using TPS introduces a 0.6% performance drop on CTW1500.

Please note the statistical bias that a considerable portion of text instances in CTW1500 are of rectangular shapes. Considering that harmonic mappings and TPS are almost identical when handling rectangular text instances, the negative impact of TPS is a lot more significant than what the number shows. Due to the same reason, we do not perform the same experiment on IC-

Table 1: Experiment results under different settings. "HM" means harmonic mappings, "SF" refers to the SVM-based filtering process, "GI" represents geometric information, and "RAE" indicates reference angle-based encoding. "P", "R", and "F" represent precision, recall, and F-measure respectively.

			HM RAE SF GI $\frac{C T W 1500}{P R F P R F}$					
			\sim $\sqrt{}$ $\sqrt{}$ 89.7 80.9 85.1			and the state of the state		
			$\sqrt{ }$ - $\sqrt{ }$ 84.9 72.5 78.2				86.0 67.4 75.6	
						\checkmark \checkmark - \checkmark 82.2 83.1 82.7 85.0 81.5 83.2		
						\checkmark \checkmark \checkmark - 86.2 83.6 84.9 87.3 83.9 85.6		
						\checkmark \checkmark \checkmark \checkmark 88.2 83.3 85.7 89.5 83.5 86.4		

DAR 2015. Since ICDAR 2015 only contains rectangular text instances, there is no significance in such experiment.

We also perform a comparison on the time complexity. To perform the same task of label generation for CTW1500, on average, the harmonic mapping-based method took 1.27 seconds per text instance, and the TPS method took 1.09 seconds per text instance. We conclude that both methods introduce runtime overheads, and TPS is faster. However, it does not affect the training efficiency, since label generation is only performed once before training. The labels are reused efficiently during training, with no run-time overhead.

4.3.2. Reference Angle-Based Encoding

In this section, we compare the reference angle-based encoding technique explained in Sec. 3.3.2 with the conventional encoding technique which utilizes Eq. 6. As shown in Tab. 1, the reference angle-based encoding technique brings performance gains of 7.5% and 10.8% on CTW1500 and ICDAR 2015 respectively. Thus, we conclude that regression heads do not work well when their target feature maps exhibit abrupt jump discontinuity (see Fig. 6 (c-d)).

4.3.3. SVM-Based Filtering and Geometric Information

To validate the necessity of our SVM-based filtering process and the geometric information introduced in Sec. 3.4.3, we perform the following experiments: (1) we compare the SVM-

Figure 11: The influence of the kernel scale. The red lines and blue lines represent the results on CTW1500 and ICDAR 2015, respectively.

based filtering process with a conventional filtering scheme, which discards any text instance with an area smaller than 10 or a confidence value lower than 0.65 ; and (2) we abandon the use of the geometric information introduced in Sec. 3.4.3, that is the distortion and aspect ratios, and evaluate the effect.

For the first experiment, as shown in Tab. 1, by including the SVM-based filtering process, we obtain a 3.0% gain on CTW1500 and a 3.2% gain on ICDAR 2015, showing the effectiveness of our filtering scheme. As for the second experiment, utilizing the additional geometric information, during the filtering process brings a 0.8% performance gain on both CTW1500 and ICDAR 2015 (see Tab. 1), proving the necessity of utilizing such information during the filtering process.

4.3.4. Kernel Scale

It is stated in [10] that text kernels should be granted thickness since a single-point line is prone to noise. And such statement has been practiced in various methods [10, 11, 13]. We are able to increase the thickness of text kernels by assigning radiuses to all kernel points during post-processing. For each text instance, the radiuses of its kernel points are equal to $s \cdot h$, where s is a constant named the kernel scale, ranging from 0 to 1, and h is the height of that text instance, given by $2r_k + 2r_e$. As shown in Fig. 11, in our case, the F-measure has a negative correlation with the kernel scale, while the inference speed is observed to have a positive correlation with the kernel scale. However, the gain in inference speed is minor. It is thus optimal to set the kernel scale to 0.

4.4. Comparisons With State-of-the-Art Methods

We compare our proposed method with previous methods on four standard benchmarks, including two benchmarks for arbitrary-shaped text, and two benchmarks for multi-oriented text

4.4.1. Detecting Arbitrary-Shaped Text

Our CTRNet demonstrates great performance and shape robustness on two arbitrary-shaped text benchmarks: Total-Text

Table 2: Experiment results on CTW1500. "Ext." indicates whether external data is used. "P", "R", and "F" represent precision, recall, and F-measure re-

spectively. * indicates the results from [18].						
Method		Ext. Venue	P	R	F	
$CTPN* [8]$		ECCV'16		$60.4*53.8*56.9*$		
$EAST* [9]$		CVPR'17	78.7*	$49.1*$	$60.4*$	
CTD+TLOC ^[18]			77.4	69.8	73.4	
TextSnake [10]		ECCV'18	67.9	85.3	75.6	
PSENet-1s $[11]$		CVPR'19	80.6	75.6	78.0	
CSE [56]		CVPR'19	81.1	76.0	78.4	
PAN-640 [13]		ICCV ₁₉	84.6	77.7	81.0	
$PSENet-1s [11]$		CVPR'19	84.8	79.7	82.2	
Text Perceptron [35]		AAA1'20	88.7	78.2	83.1	
DB-ResNet50 [12]		AAA1'20	86.9	80.2	83.4	
CTRNet			88.6	79.0	83.5	
PAN-640 [13]		ICCV'19	86.4	81.2	83.7	
CTRNet			88.2	83.3	85.7	

Table 3: Experiment results on Total-Text. "P", "R", and "F" represent precision, recall, and F-measure respectively. * indicates the results from [10].

Method	Venue	P	R	F
EAST* $[9]$	CVPR'17	$50.0*$	$36.2*$	$42.0*$
TextSnake [10]	ECCV'18	82.7	74.5	78.4
CSE [56]	CVPR'19	81.4	79.1	80.2
PSENet-1s [11]	CVPR'19	84.0	78.0	80.9
Text Perceptron [35]	AAA1'20	88.1	78.9	83.3
Boundary [29]	AAA1'20	85.2	83.5	84.3
DB-ResNet50 [12]	AAAI'20	87.1	82.5	84.7
PAN-640 [13]	ICCV'19	89.3	81.0	85.0
CTRNet		88.4	82.9	85.6

Table 4: Experiment results on MSRA-TD500. "P", "R", and "F" represent precision, recall, and F-measure respectively

and CTW1500.

As shown in Tab. 2 and Tab. 3, our method consistently outperforms previous methods by a large margin, in terms of F-measure. Specifically, CTRNet outperforms the previous state-of-the-art methods by 2.0% and 0.6% on CTW1500 and Total-Text respectively, demonstrating the superiority of CTR-Net when detecting arbitrary-shaped text.

Moreover, when training from scratch on CTW1500, compared with other results that do not rely on external data, CTR-Net outperforms the most accurate method PAN-640 by 2.5%. Notably, it is only 0.2% behind the previous state-of-the-art method, which is trained with external data, proving the outstanding robustness of our method.

It is worth noting that, compared with PSENet-1s, whose network architecture is almost identical to ours, CTRNet brings huge improvements of 3.5% on CTW1500 and 4.7% on Total-Text. Such improvement is a solid proof for the validity of CTRs and our post-processing algorithm.

4.4.2. Detecting Multi-Oriented Text

Experiments on MSRA-TD500 and ICDAR 2015 show that CTRNet is robust when detecting multi-oriented text.

On MSRA-TD500, as shown in Tab. 4, CTRNet outperforms the state-of-the-art methods by 0.5%. Specifically, it surpasses PAN and TextSnake, which relies heavily on text kernel segmentation, by solid 1.3% and 7.1%. Such results prove the great consistency of CTRNet and the advantage of omitting text kernel segmentation.

For ICDAR 2015, it can be observed in Tab. 5 that CTRNet achieves state-of-the-art performance and is second only to DB-

Figure 12: Qualitative results of CTRNet. Each section includes the detection result (left), kernel visualization (top right), and reconstruction result (bottom right).

ResNet50 (1152). However, it is not a fair comparison since DB-ResNet50 (1152) receives input images with height 1152, which is far larger than the input images of CTRNet. When instead compared with DB-ResNet50 (736), whose input size is similar to ours, CTRNet surpasses it by 1.0%. Further, when compared with PSENet-1s, which differs from us only in label design and post-processing, CTRNet yields an increase of 0.7%, showing the solid improvement that our label design and post-processing algorithm bring.

Please note that no specific trick, such as minimal area rectangles fitting, is implemented when handling MSRA-TD500 and ICDAR 2015, whereas some of the methods [11, 13] do. Still, the results on multi-oriented text datasets demonstrate the great consistency and robustness of CTRNet. Moreover, experiment results on MSRA-TD500 show that CTRNet is exceptionally effective when handling long text instances.

Table 5: Experiment results on ICDAR 2015. The values within parentheses indicate the height of the input image. "P", "R", and "F" represent precision, recall, and F-measure respectively.

Method	Venue	P	R	F
CTPN [8]	ECCV'16	74.2	51.6	60.9
EAST $[9]$	CVPR'17	83.6	73.5	78.2
RRPN [25]	TMM'18	82	73	77
RRD [24]	CVPR'18	85.6	79.0	82.2
PixelLink [33]	AAI'18	82.9	81.7	82.3
TextSnake [10]	ECCV'18	84.9	80.4	82.6
PAN [13]	ICCV'19	84.0	81.9	82.9
Boundary [29]	AAA1'20	88.1	82.2	85.0
DB-ResNet50 (736) [12]	AAA1'20	88.2	82.7	85.4
CSE [56]	CVPR'19	92.3	79.9	85.7
PSENet-1s $[11]$	CVPR'19	86.9	84.5	85.7
Text Perceptron [35]	AAA1'20	91.6	81.8	86.4
DB-ResNet50 (1152) [12]	AAA1'20	91.8	83.2	87.3
CTRNet		89.5	83.5	86.4

Table 6: Overall results on all four benchmark datasets. "F" represents Fmeasure. "SVM", "Post.", and "Total" indicate the average time consumption of the SVM module, the post-processing algorithm, and the inference pipeline as a whole

Dataset	F	Time(s)				
		SVM	Post.	Total		
CTW1500	857	4.83×10^{-4}	0.154	0.191		
Total-Text	85.6	5.26×10^{-4}	0.092	0.127		
MSRA-TD500	854	1.24×10^{-4}	0.072	0.103		
ICDAR 2015	864	1.98×10^{-4}	0.060	0.108		

4.5. Overall Results and Running Time Analysis 4.5.1. Overall Results

Qualitatively, it can be observed in Fig. 12 that through elaborate label design, our CTRNet generates stable and accurate predictions for text kernels, without the need of directly segmenting them. Meanwhile, CTRNet consistently produces accurate and shape-robust detection results when handling horizontal text, multi-oriented text, and arbitrary-shaped text. Quantitatively, it can be observed in Tab. 6 that CTR-Net consistently achieves excellence on all four of the datasets. Notably, to the best of our knowledge, CTRNet is among the first methods to achieve F-measures higher than 85.0% on all these datasets, which proves the solid superiority of CTRNet, in terms of accuracy and consistency.

4.5.2. Running Time Analysis

We use a single RTX2080Ti GPU and the Dual Intel Xeon E5-2650 v4 $@$ 2.20GHz processor for running time analysis. As shown in Tab. 6, it takes an average of 0.132 seconds for CTRNet to process an image. While the SVM module poses unnoticeable time cost, the post-processing as a whole generally takes up more than 70% of the inference time. However, it is worth noting that unlike other segmentation-based methods that implement the post-processing algorithms using the more efficient C++, such as PSENet-1s, our post-processing algorithm, for the purpose of this study, is implemented purely in Python.

Nevertheless, the inference speed of CTRNet is still significantly higher than a large set of recent methods [10, 11, 56], including PSENet-1s.

To carry out a fair comparison, we implement PSENet-1s using its open-sourced official implementation, under our hardware environment. According to our tests on CTW1500, its average running time for each picture is 0.334 seconds. It is slower than CTRNet, which takes 0.191 seconds under the same experimental configuration. This shows that CTRNet has a competitive running time performance.

5. Conclusion

In this paper, we propose an effective framework to detect arbitrary-shaped text with outstanding accuracy and stability. We first introduce Conceptual Text Regions, a class of cognition-inspired tools for elaborate label generation. Further, we propose a well-designed inference pipeline to predict text instances using the geometric features generated by CTRs. The fact that CTRs allow for sophisticated label design and that the inference pipeline omits the need for text kernel segmentation establishes CTRNet as a robust and accurate arbitrary-shaped text detector. Achieving F-measures greater than 85.0% on all four of CTW1500, Total-Text, MSRA-TD500, and ICDAR 2015, CTRNet demonstrates superior advantages in terms of accuracy and consistency when compared with previous stateof-the-art text detectors.

For future study, we consider it meaningful to investigate the possibility of establishing the CTR method as a universal text label generation technique. It is also of interest to utilize the potential of CTRs and evolve CTRNet into an end-to-end trainable text recognition framework. Last but not least, we will seek to utilize deep reinforcement learning and multi-task learning algorithms [57, 58, 59, 60] to optimize the generalization capability of such text recognition framework.

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