

Particle-scale interaction in sand-rubber mixtures and their influence on energy dissipation mechanisms

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ABSTRACT

Sand-rubber mixture (SRm) behaviour is affected by rubber content (RC) whilst dissipation in sands is caused by inter-particle sliding. Dissipation in SRm is as, or more significant than in sands. However, the mechanisms of dissipation in SRm are not well understood. In this study, one-dimensional compression tests on sand samples with RC of 0%, 15%, 30%, 45% and 100% by mass were performed on a standard oedometer. In addition, a SRm with RC of 30% was tested on a mini-oedometer placed inside an X-ray scanner and 3D images of the internal structure of the material were acquired at three stages during loading and unloading. Image analysis was used to infer particle-scale measurements and provide experimental evidence to help explaining the energy dissipation mechanisms for SRm. It is postulated here that energy dissipation in these mixtures is dominated by inter-particle sliding at initial stages of loading, but once rubber particles fill the voids spaces between the sand, deformation and dissipation mechanisms are dominated by the deformation of the rubber particles.

KEYWORDS

Fabric/structure of soils; Particle-scale behaviour; Sand-rubber mixtures; Compressibility; Microscopy; Laboratory tests

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INTRODUCTION

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2 Previous research on the behaviour of sand-rubber mixtures (SRm) has demonstrated that using tyre
3 shreds can lead to shear strength increases (e.g. Edil & Bosscher, 1994; Foose et al., 1996; Zornberg
4 et al., 2004; Mashiri et al., 2015a; Mashiri et al., 2015b; Fu et al., 2014; Fu et al., 2017). On the other
5 hand, when rubber crumbs were used a decrease in shear strength was observed (e.g. Masad et al.,
6 1996; Youwai & Bergado, 2003; Sheikh et al., 2012). An increase in the rubber content is believed to
7 be associated to a reduction in the stiffness of the material (e.g. Zheng-Yi & Sutter, 2000;
8 Anastasiadis et al., 2012; Senetakis et al., 2012; Nakhaei et al., 2012; Ehsani et al., 2015; Pistolas et
9 al., 2018). In fact, variations in rubber content can result in rubber-like or sand-like behaviours (Lee et
10 al. 2007; Lee et al., 2014; Kim & Santamarina, 2008; Senetakis & Anastasiadis, 2015).

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12 Existing evidence considers the dynamic behaviour of SRm under less than 10 loading-unloading
13 cycles. The consensus is that energy dissipation in SRm is as, or more significant than in sands (e.g.
14 Zheng-Yi & Sutter 2000; Senetakis et al., 2012; Ehsani et al., 2015).

15
16 In summary, geotechnical properties of SRm are affected by rubber content, particle size, particle
17 shape, and size ratio between compressible and rigid particles, amongst other factors. However,
18 experimental evidence at the particle scale is very limited. This study aims to gain further
19 understanding on the particle-scale mechanisms that underlie the observed energy dissipation
20 mechanisms of RSm. The effect of rubber particle shape was qualitatively assessed by means of plane
21 strain tests on mixtures of rubber particles and acrylic discs. On the other hand, the influence of
22 rubber content is evaluated via standard oedometer tests on SRm. Finally, grain-scale measurements
23 of a mini-oedometer sample carried out on a SRm with 30% RC are presented in order to quantify
24 changes of contact area between sand and rubber particles under different loading regimes. This set of
25 experiments is then discussed to provide further insight into the potential microscale mechanisms that
26 underlie energy dissipation in SRm.

PLAIN STRAIN EXPERIMENTS

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28 Plane strain models of acrylic discs mixed with rubber particles of different shapes and sizes were
29 developed to preliminarily observe particle scale interaction mechanisms in SRm. In order to make
30 qualitative observations on the effect of the rubber particle shape, two rubber particle aspect ratios
31 were used in conjunction with acrylic discs of 6 mm diameter as shown in Figs. 1 and 2. Rubber
32 crumbs (Fig. 1) had an aspect ratio (AR) between 1.0 and 1.5 while the size ratio (SR) between rubber
33 and acrylic discs was approximately 1.0. Rubber shreds (Fig. 2) had an aspect ratio (AR) between 5
34 and 6 while the size ratio between shreds and acrylic discs varied between 2 and 3. The plane strain
35 apparatus for the experiments shown in Figs. 1 and 2 consisted of an A4-size acrylic sheet with PVC
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1 flat bars used as lateral boundaries. Two vertical flat bars of made PVC of 20 mm width and 2 mm
2 thickness were fixed to the sides of the acrylic base using screws to provide lateral constraint. A
3 similar PVC flat bar was fixed horizontally to the bottom in order to provide a fixed base to the
4 particles. Loading in the vertical direction was carried out by moving an additional “top” PVC bar
5 attached to a sliding slot along the lateral (fixed) boundaries that enabled accurate control of the
6 specimen’s vertical dimension and provided a constant normal stress. Due to the geometry of the
7 rubber and acrylic particles any deformations in the out of plane direction are prevented and plane
8 strain conditions are guaranteed. Fig. 1 shows a mix of mono-disperse acrylic discs mixed with rubber
9 crumbs before (Fig. 1a) and after compression (Fig. 1b) under a nominal one-dimensional load and
10 lateral deformation constraint. It can be seen that during loading the area of contact of rubber particles
11 with acrylic and other rubber particles increases. This is evidenced by changes in the shape of the
12 rubber crumbs at the boundary between rubber particles and acrylic discs.
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21 Fig. 2 shows the effect of loading on the behaviour of an assembly of acrylic discs and shredded
22 rubber particles. The material, sample preparation and loading are equal to those used for crumbs.
23 Hence, differences are due to rubber particle only. By comparing Fig. 2a and Fig. 1a observations on
24 the initial density can be made. The specimen with rubber shreds has a higher void ratio than that
25 made with rubber crumbs. Fig. 2b shows that during loading the rubber shreds have deformed and by
26 wrapping around the acrylic discs the contact area between rubber and acrylic has increased with
27 respect to the conditions in Fig 2a. Note that not all rubber shreds deform in equal manner. The
28 increased contact area is not homogeneous and/or proportionally equivalent across all rubber shreds.
29 This indicates the existence of a non-homogeneous stress transmission between particles (i.e. force
30 chains). Furthermore, by comparing Fig. 1b and Fig. 2b we can state that the mechanisms of stress
31 transmission at inter-particle contacts in rubber shreds are significantly different to those observed in
32 rubber crumbs. The qualitative changes observed are more significant in rubber shreds than in rubber
33 crumbs. This justifies the detailed experimental investigation using SRm with rubber shreds that
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47 **MACROSCALE BEHAVIOUR OF SRm FROM OEDOMETER TESTS**

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49 A series 100 mm diameter oedometer tests using (air pluviated) sand-rubber mixtures with shredded
50 rubber particles were performed. Sub-angular Leighton Buzzard sand particles (LBS) with a mean
51 particle diameter of 0.85 mm were mixed with recycled devulcanised shredded rubber particles at
52 rubber contents of 0%, 15%, 30% and 45% by mass. Shredded rubber particles with particle diameter
53 similar to that of the sand were used. The length of the shredded particles varied between 1 mm and 6
54 mm.
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1 Fig. 3 shows the one-dimensional (oedometric) behaviour of the SRm. The response of the sand-only
2 sample is unsurprisingly stiffer than that of any SRm, and even at large stress levels the amount of
3 vertical deformation is limited and the stress-strain response is nearly linear. We refer to this as “sand-
4 like” response. In contrast, for RC of 100% the vertical strain is significant, dependent on stress level
5 and the stress-strain response in addition to being significantly non-linear, shows clear evidence of
6 plastic deformation. We refer to this behaviour as “rubber-like” response. These patterns of behaviour
7 have also been observed in previous studies (e.g. Lee et al., 2010; Kim & Santamarina, 2008).
8 Traditionally, the magnitude of energy dissipation is calculated by estimating the area of an hysteresis
9 loop in the shear stress vs shear strain space. In order to do this with the data presented in Fig. 3 an
10 assumption regarding the value of the coefficient of earth pressure at rest (K_0) would be required.
11 Nevertheless, the area between each loading-unloading loop in Fig. 3 is a measure of energy
12 dissipation, but comments can only be made in relation to the nature of energy dissipation (i.e. shape
13 of the loading/unloading loops in Fig. 3). Fig. 3 demonstrates that energy dissipation is dependent on
14 rubber content and stress level. As a matter of interest, the dissipation of energy in all samples is
15 higher during the first loading-unloading cycle. This is confirmed by a larger accumulation of plastic
16 deformation during the first cycle in comparison with subsequent cycles. This suggests that the
17 mechanisms involved in energy dissipation are also dependent on the void ratio.

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29 With reference to Fig. 3 and as discussed before, all specimens exhibit a larger magnitude of
30 dissipation during the first loading/unloading cycle (as evidenced by a larger accumulation of plastic
31 deformation). This phase can be explained for both sand only and SRm specimens in terms of particle
32 re-arrangement and sliding at interparticle contacts (Zheng-Yi & Sutter, 2000; Anatsiadis et al.,
33 2012). On the other hand the linearity of the sand-like response is explained by the inability of sand
34 grains to slide back to their original position during unloading. Changes in void ratio are limited in
35 subsequent loading/unloading cycles. In contrast, the non-linearity and dependence of the rubber-like
36 response on stress level and rubber content can be explained by the deformability of the compressible
37 particles. During the first loading/unloading cycle dissipation is likely to occur due to particle sliding.
38 However, in subsequent cycles as the stress level increases the compressible particles deform more
39 significantly. As this happens the volume of voids reduces (filled by deformed rubber particles) and
40 the contact area increases between both rubber and sand particles. Rubber particles can then fulfil two
41 different roles: one which participates in the loading transmission and the other which acts like a void
42 inert portion (Platzer et al., 2018). Whilst the behaviour of rubber particles can be expected to be
43 nearly elastic, the inter-particle friction in rubber is significantly high (e.g. Lopera Perez et al., 2016).
44 As a result, as contact area increases with stress level, the high inter-particle friction does not enable
45 dissipation to occur due to inter-particle sliding. Energy dissipation therefore can only be explained in
46 terms of the changes of void ratio in the specimen during the loading/unloading cycles, which is in
47 turn caused by the deformability of rubber particles and their void filling capacity during loading.
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1 The microscale experiments described in the next section have been developed to provide
2 experimental evidence that supports these postulates.

3 4 **MICROSCALE QUANTIFICATION**

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6 In order to validate the hypotheses postulated above, a microscale investigation was carried out on a
7 rubber-sand mixture (30% rubber by mass) composed of the same sand and shredded rubber particle
8 types used in the previous oedometer tests. A mini-oedometer with an internal diameter of 14mm was
9 operated inside an X-ray scanner in order to obtain images of the internal microstructure of the
10 mixtures as they deform under loading and unloading. The X-ray scanner system used was a Nikon
11 XTH 225 ST located at the Research Centre at Harwell, Oxfordshire (UK). The experimental set-up
12 consisted of a load cell, a vertical piston, a micrometer and a small oedometer. The set-up was
13 designed for this particular scanner and was mounted on the rotating table of the scanner, more details
14 on the equipment can be found in Nadimi & Fonseca (2018). The size of the specimen was 14 mm in
15 diameter and 11 mm high. The force was exerted by manually screwing the micrometer until the pre-
16 set load was reached. A high precision micrometer with an axial loading capacity of 450 N was used.
17 The sample container was made of Perspex with 2 mm thickness for which a value of less than 3 μm
18 deflection under the maximum applied force was measured. The lateral friction has been minimized
19 by allowing a 1 mm gap between the container and the X-ray window. The exerted force was
20 monitored by a low profile ‘pancake type’ load cell with a 500 N capacity.

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22 The images were acquired at three stages: prior to loading (Stage 0), under a vertical load of 120N
23 (Stage 1) and after unloading to 35N (Stage 2). A total of 3142 projections were collected per scan,
24 with an exposure of 500 ms per projection. The 3D images acquired had a resolution of 9.2 μm
25 (length of voxel edge). In an X-ray scanning, the objects within the sample attenuate different levels
26 of X-ray beam energy, depending on the material composition and density. Denser materials, the
27 sand, attenuate more than less dense materials, the rubber and void space, and this difference in
28 attenuation is represented by the intensity values of the voxels (volumetric pixels). The contrast of
29 intensity level allows for differentiation of the three phases within the image, shown in Fig. 4. The
30 rubber (darker grey) has intensity values between the void (black) and the sand grains (brighter grey).

31
32 An in-house imaging processing code was developed in Matlab (Mathworks, 2018) to segment the
33 images by separating the three phases. This includes a two-step binarisation using Otsu’s thresholding
34 (Otsu, 1979), for which the sand phase was first isolated and secondly the rubber phase was separated
35 from the void space. Horizontal and vertical sections through the 3D segmented images at the three
36 stages of loading are presented in Fig. 5. The subsequent step of image processing was to identify the
37 contacts between the sand grains and the rubber (Fonseca at al., 2013). The measurements consisted
38 in counting the number of voxels forming each of the three phases and the contact regions. The
39 volumes of sand, rubber and void space were obtained by multiplying the number of voxels by the
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1 voxel size $(9.2\mu\text{m})^3$. For the contact areas the number of voxels was multiplied by $(9.2\mu\text{m})^2$ to obtain
2 the area of surfaces.

3
4 Table 1 shows the height of the sample, measured from the 3D images, at the three stages and the void
5 ratio. The void ratio (e_{im}) was calculated as:

$$6 \quad e_{im} = \frac{N_{void}^{voxel}}{N_{sand}^{voxels} + N_{rubber}^{voxels}} \quad (1)$$

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9 where N_{void}^{voxel} is the number of voxels forming the void space within the sample, N_{sand}^{voxels} is the number
10 of voxels occupied by sand grains and N_{rubber}^{voxels} is the number of voxels occupied by rubber.

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16 The evolution of the rubber volume under loading and unloading is presented in Fig. 6 together with
17 the evolution of the sample void ratio. It can be seen that the rubber undergoes volumetric
18 compression when the loads increases to 120 N and on unloading to 35 N almost all the deformation
19 is recoverable, as expected. The evolution of the contact area between the sand grains and the rubber
20 is presented in Fig. 7. In this case, we can see an increase in the contact area as the applied load
21 increases and on unloading only part of the newly formed contact areas are lost. This is an interesting
22 finding and it appears to mimic (qualitatively) the evolution of the void ratio.

23 24 25 26 27 28 **DISCUSSION AND CONCLUSIONS**

29
30 Results obtained from a mini-oedometer inside an X-ray scanner have indicated that the contact area
31 between sand and shredded rubber particles increases upon loading and only very slightly reduces
32 during unloading. Similar observations were made in terms of void ratio. This occurs with very high
33 inter-particle friction at contacts of rubber particles. Hence energy dissipation mechanisms at the
34 macro-level are the result of physical phenomena at the micro-level. It has been shown that the
35 common dissipation mechanism in sands (i.e. inter-particle sliding) only occurs during the initial
36 loading-unloading cycle for SRm. After this point rubber particles “lock” and their deformation and
37 void-filling capacity dominates the dissipation mechanisms. These mechanisms have been postulated
38 based on quantitative image analysis, but also based on standard oedometers tests on SRm comprised
39 of Leighton Buzzard sand and rubber shreds following preliminary analyses on plane strain models of
40 acrylic discs and rubber particles of different shapes. The results across the three different
41 experimental set-ups support the authors’ hypotheses and provide an explanation of the micro-scale
42 interactions affecting the observed macro-scale behaviour.

43 44 45 46 47 48 49 50 51 52 53 **REFERENCES**

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Fig 1. Compression test on sand mixed with crumb rubber particles (a) before loading and (b) during loading

Fig 2. Compression test on sand mixed with shredded rubber particles (a) before loading and (b) during loading

Fig 3. Behaviour of SRm at different percentage (by mass) of rubber content in oedometer tests

Fig. 4: Tomographic image of the sample prior to loading: (a) cross sectional view and (b) vertical section

Fig. 5: Views through the segmented images with the three phases differentiated: sand in dark blue, rubber in light blue and void in white. Horizontal sections at (a) Stage 0, (b) Stage 1 and (c) Stage 2; and vertical sections at (d) Stage 0, (e) Stage 1 and (f) Stage 2

Fig 6: Evolution of the volume of rubber under loading and unloading and comparison with the evolution of the overall void ratio of the sample

Fig. 7: Evolution of the contact area under loading and unloading and comparison with the evolution of the overall void ratio of the sample

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Table 1: Measurements of sample height and global void ratio of the sample at the three stages, obtained from the 3D images

NOTATION LIST

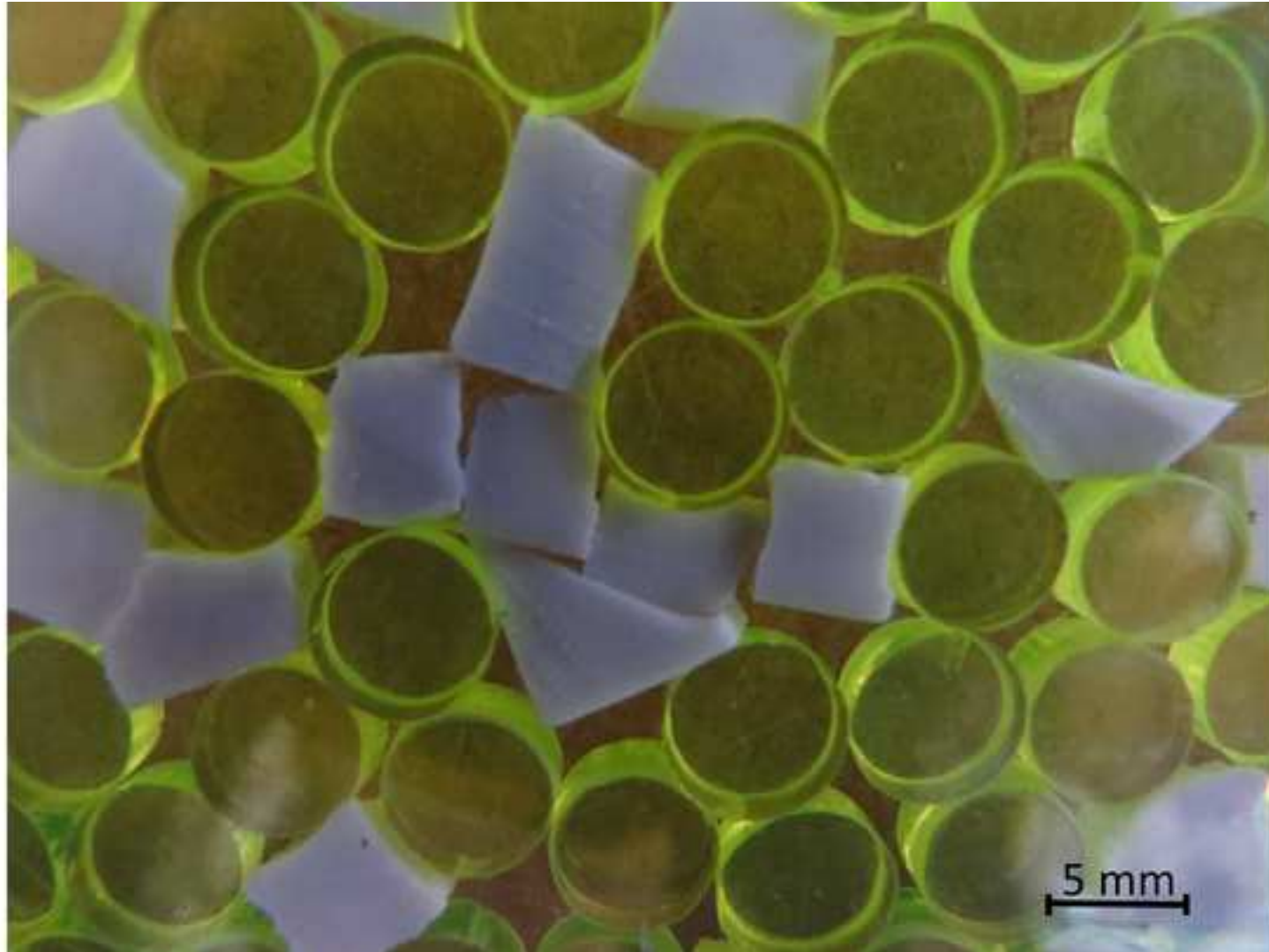
e_{im} void ratio measured from the 3D images

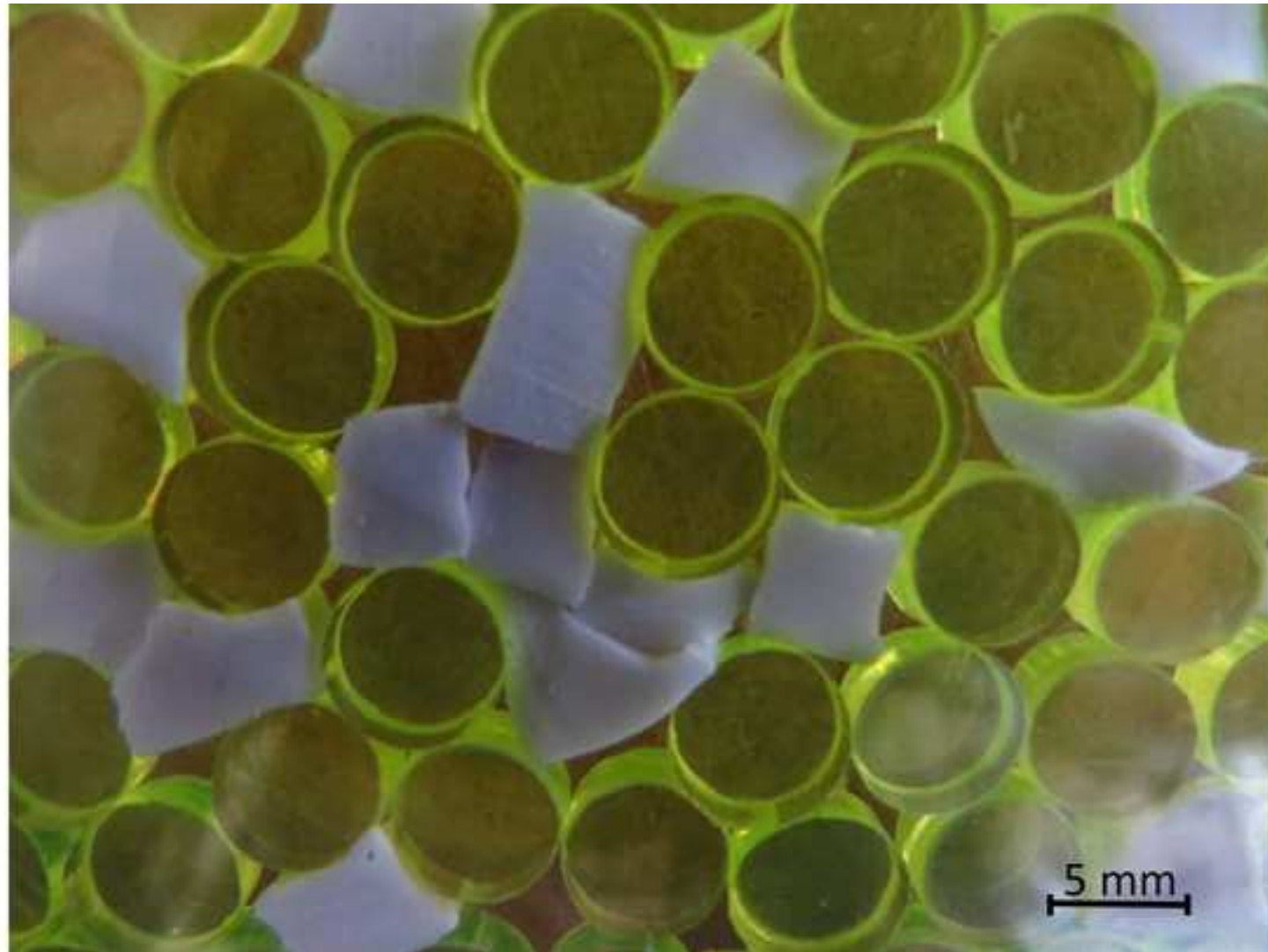
N_{voxel}^{void} number of voxels forming the void space within the sample

N_{voxels}^{sand} number of voxels occupied by sand grains

N_{voxels}^{rubber} number of voxels occupied by rubber

	Stage 0	Stage 1	Stage 2
Load (N)	0	120	35
Sample height (mm)	11.14	10.24	10.51
Void ratio (e_{im})	0.441	0.345	0.358





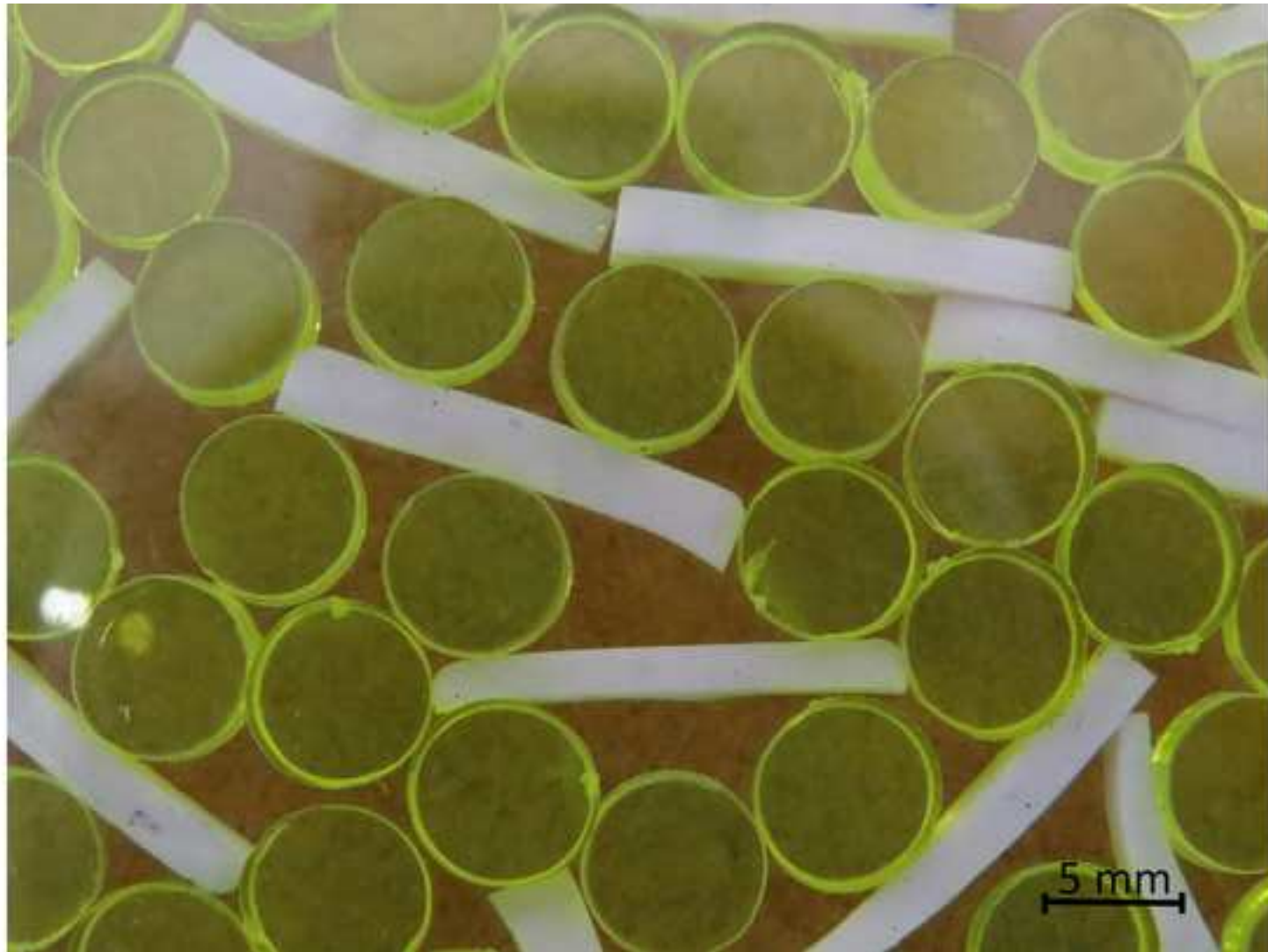
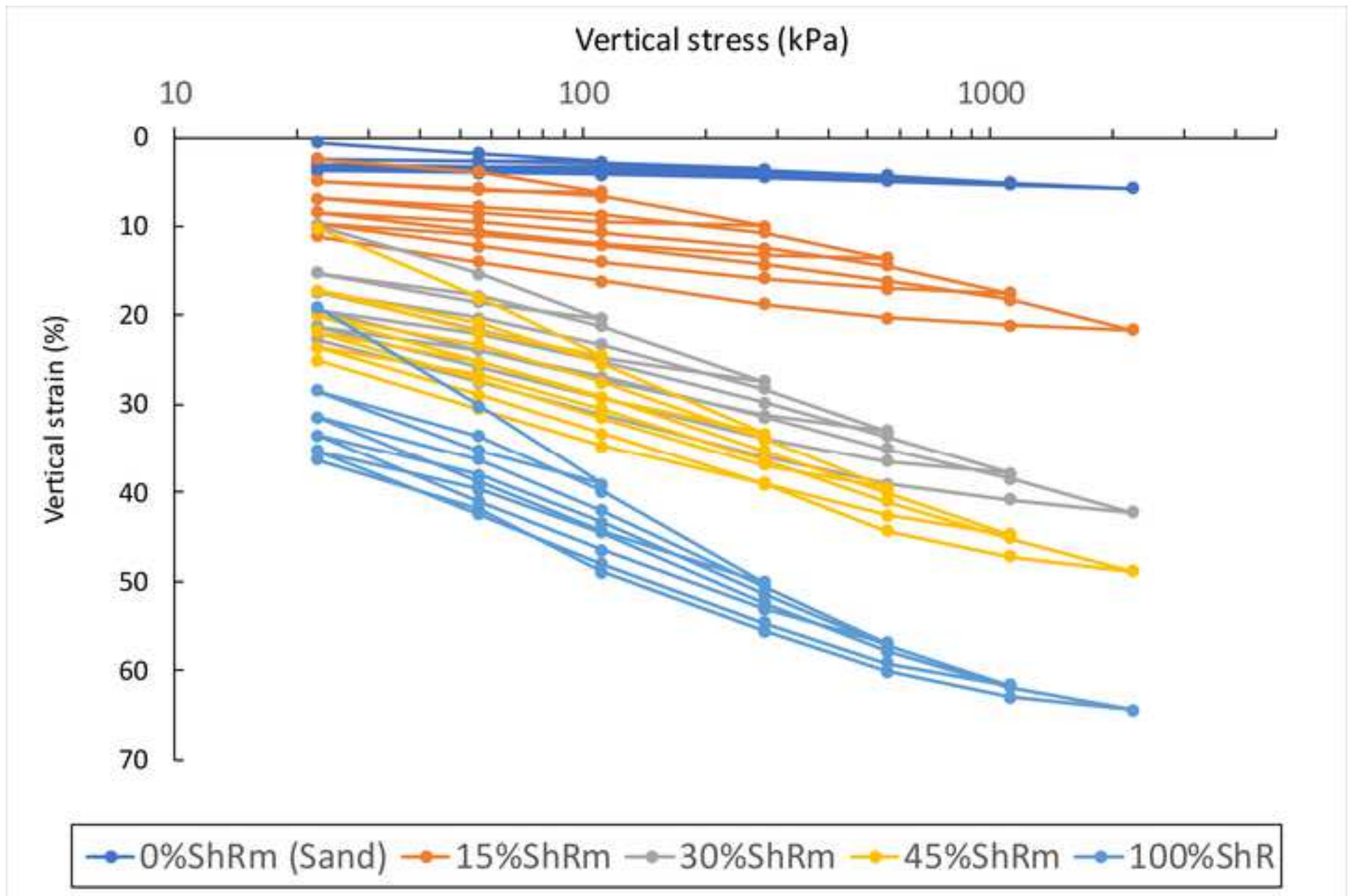
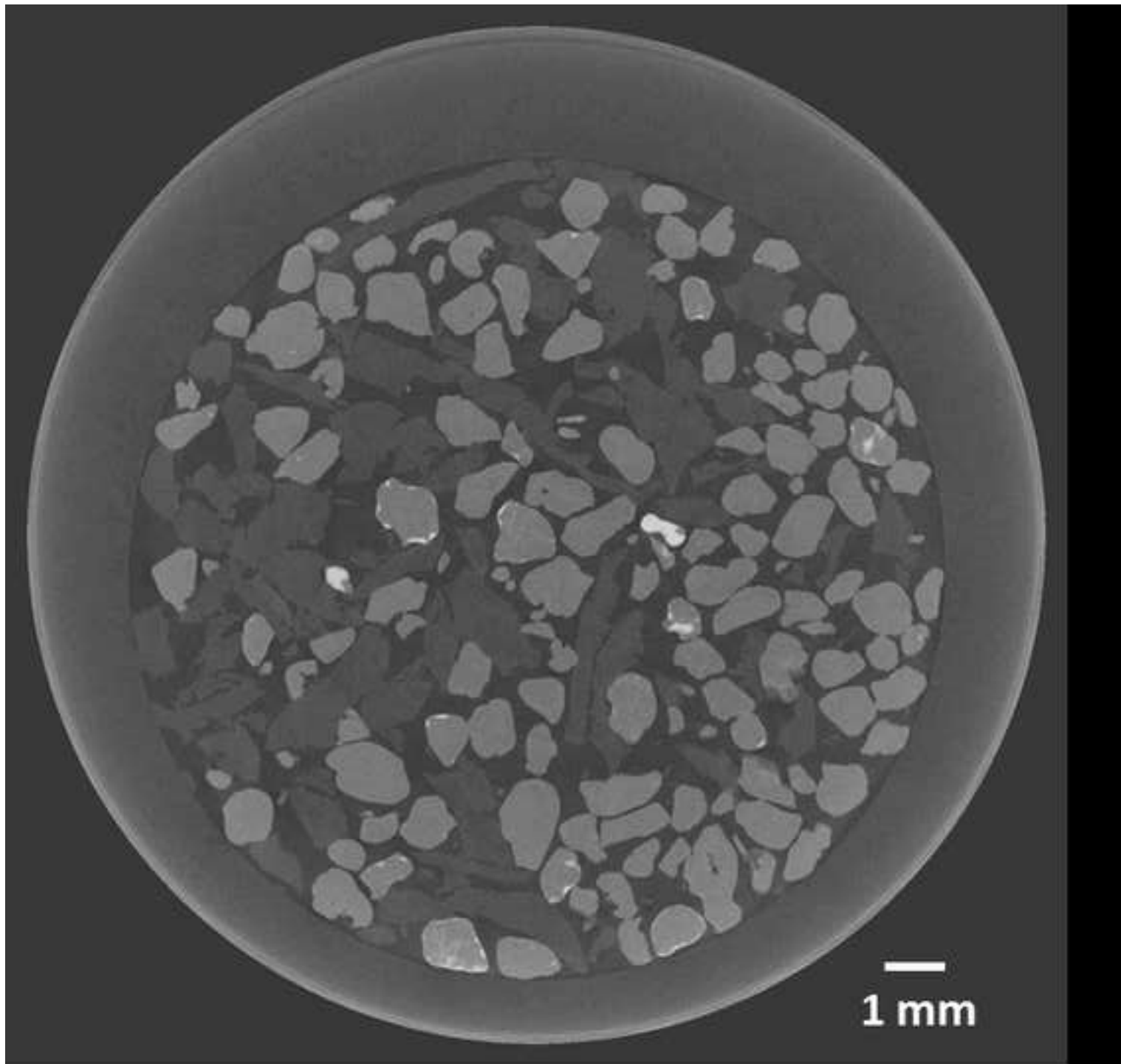
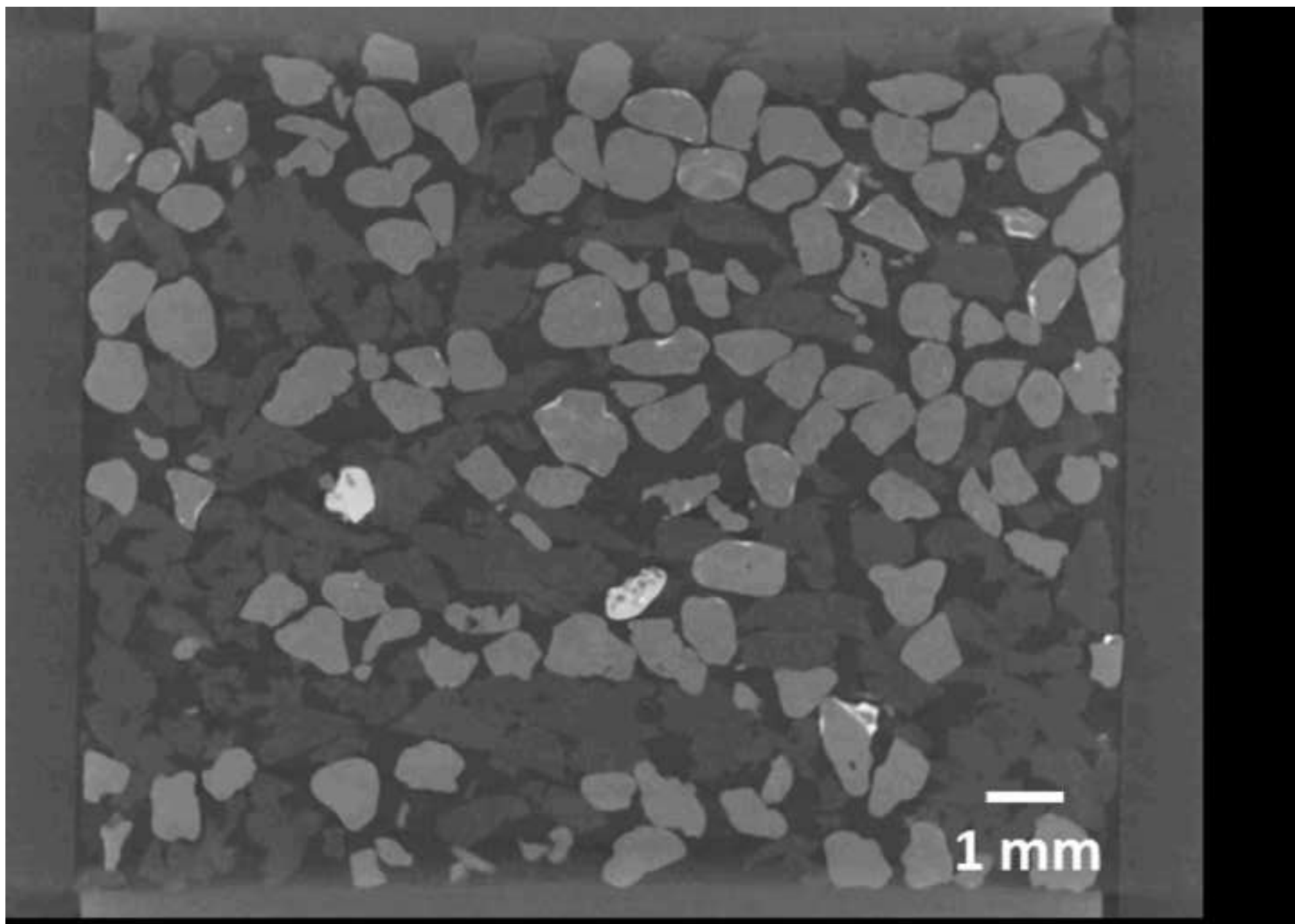


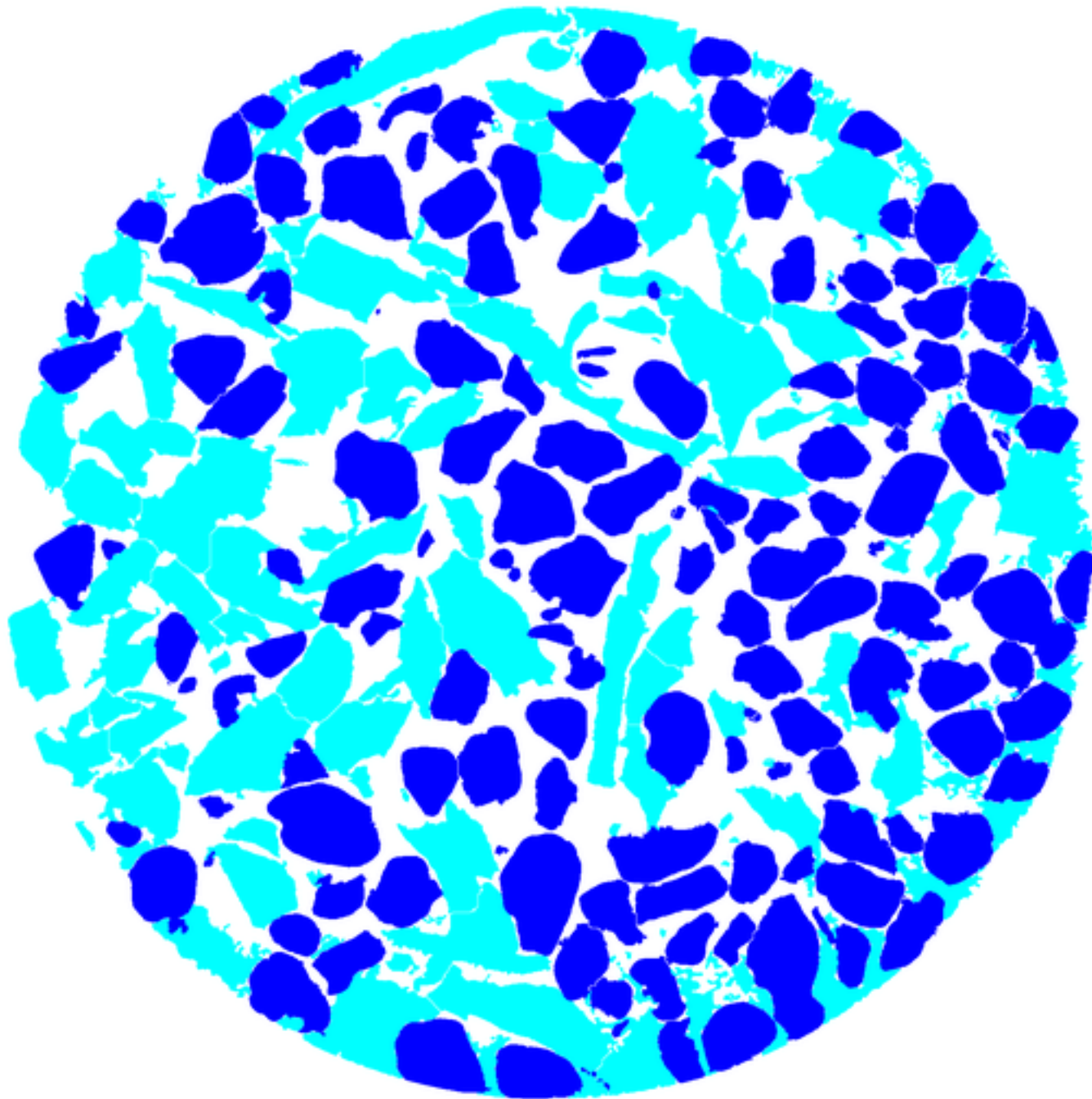


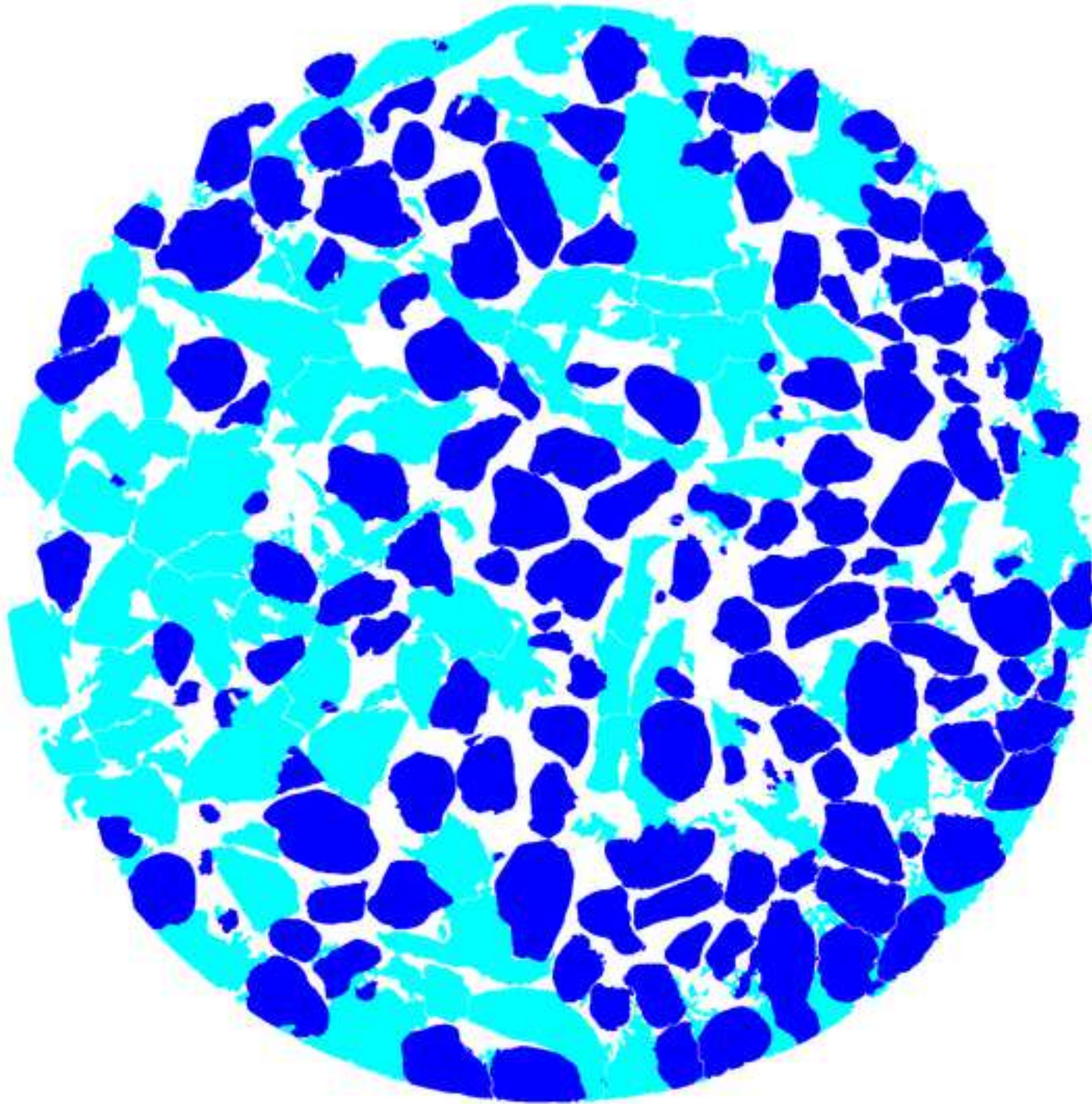
Figure 3

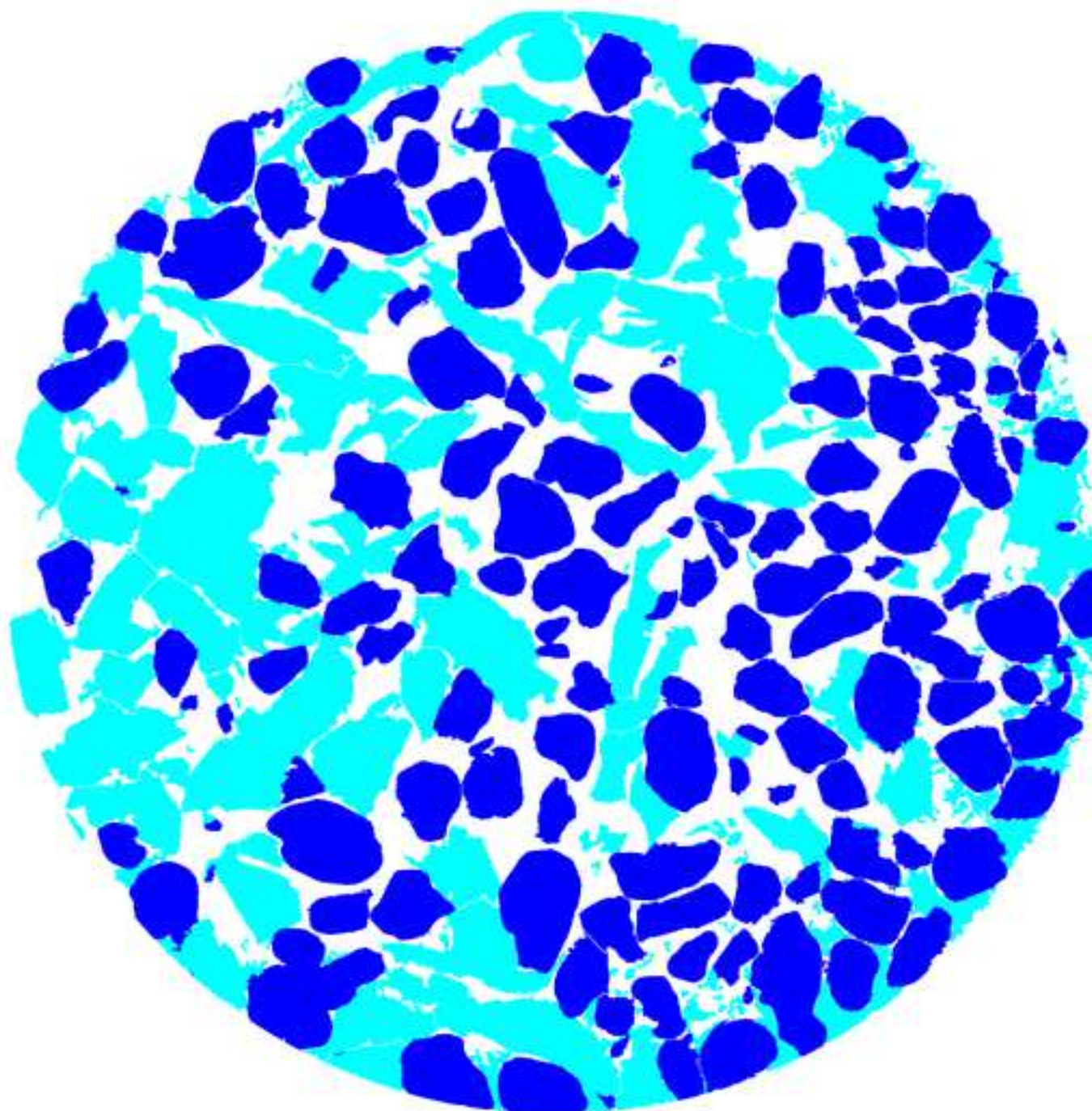


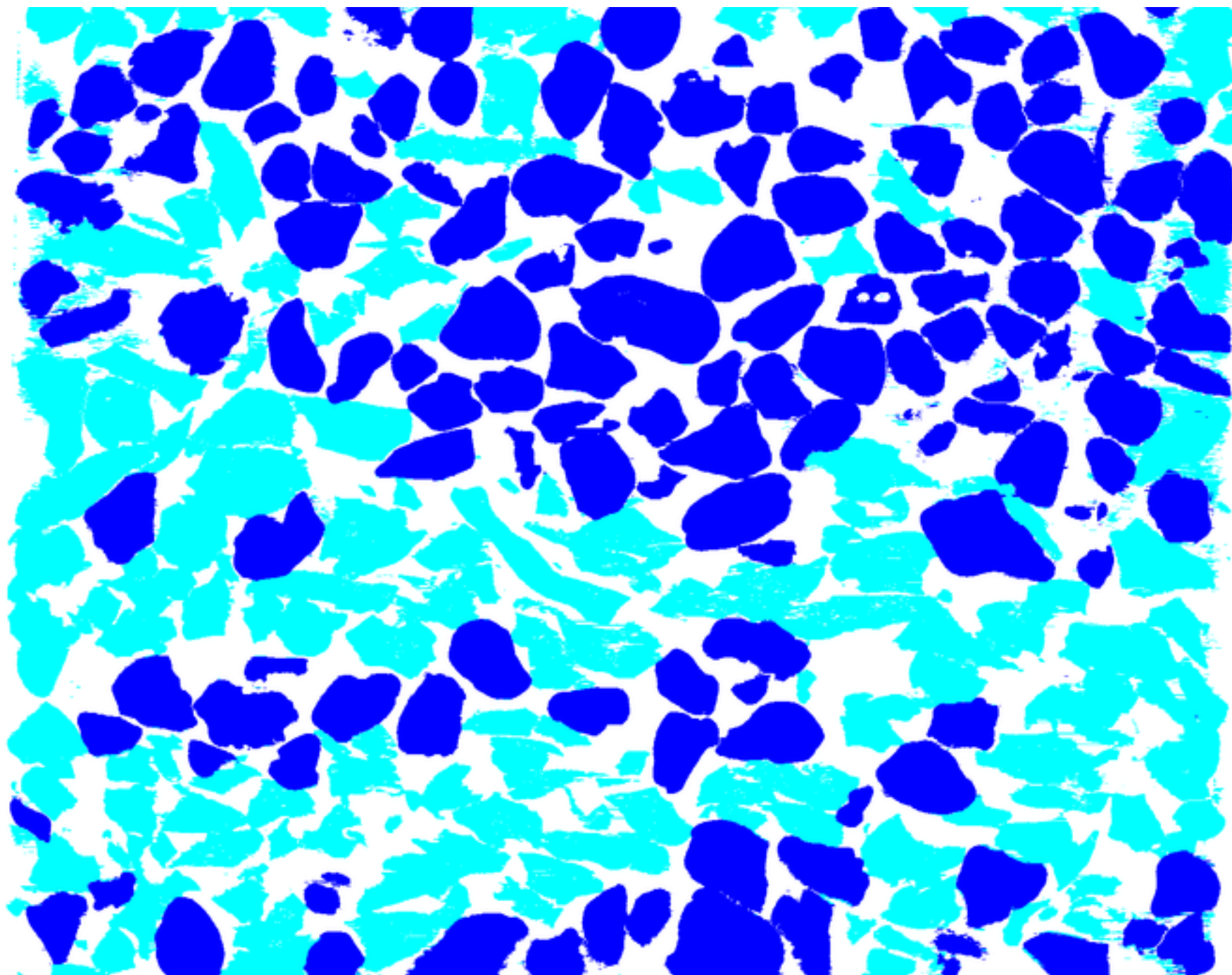


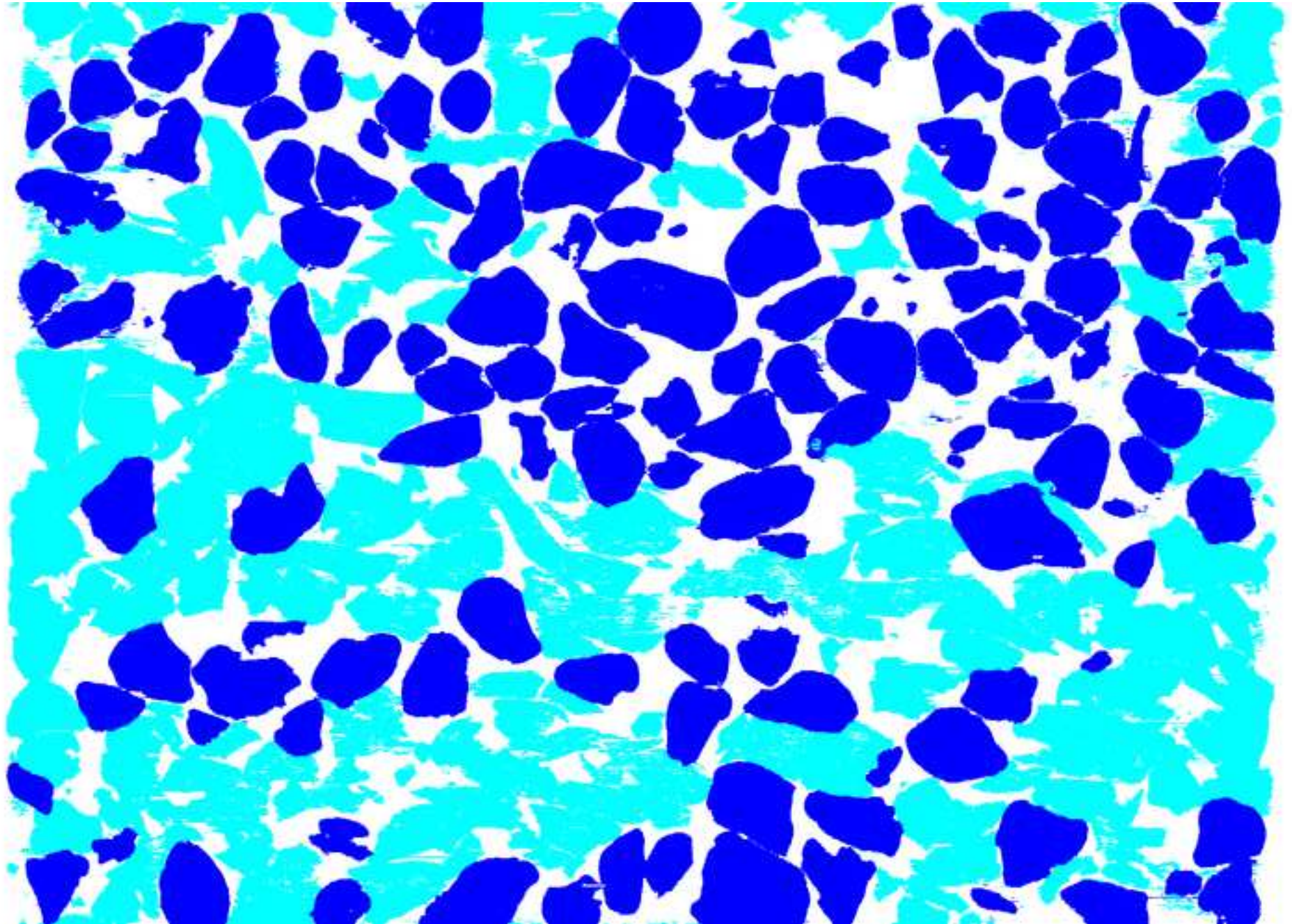


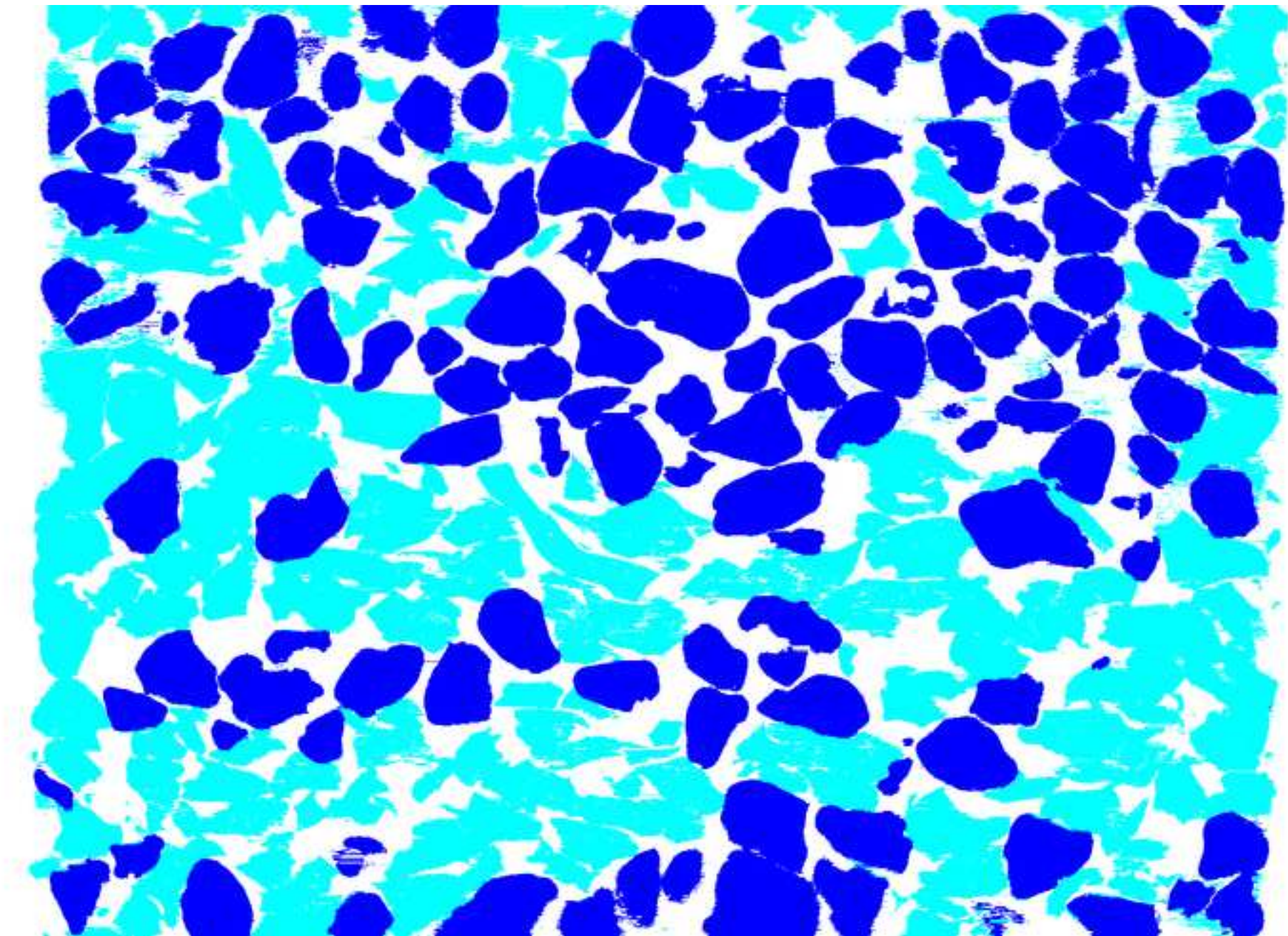


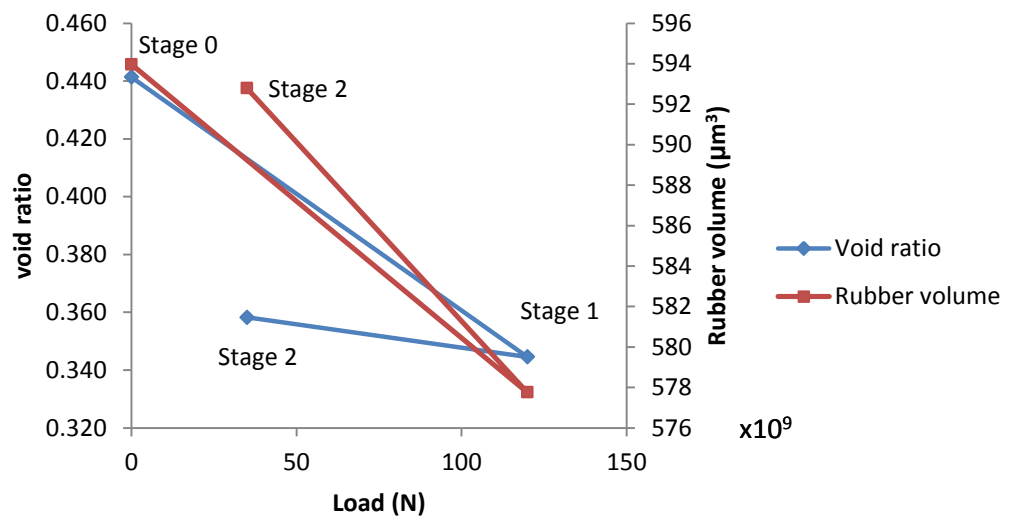


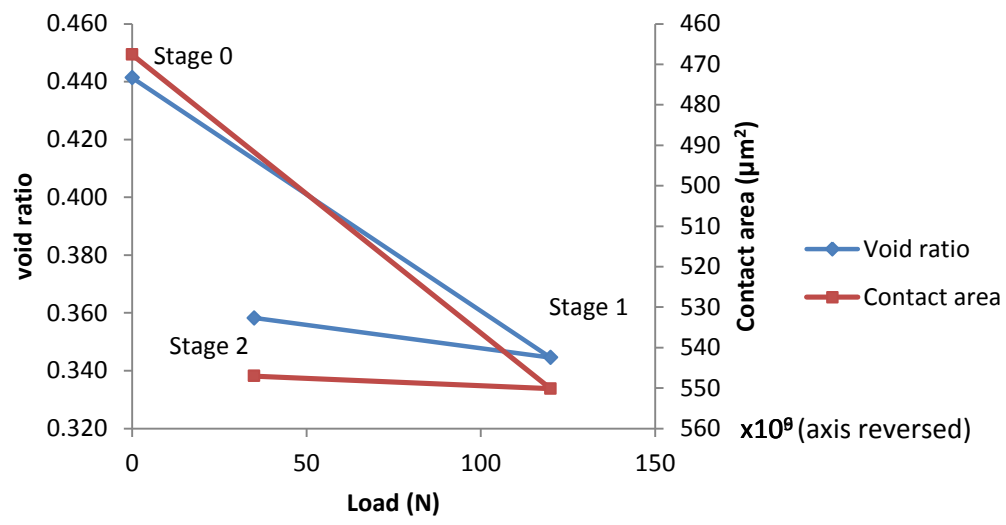














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